

Find The 8th Term In The Sequence $-\frac{1}{2}, -1, -2, -4, \dots$

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Understanding sequences and their patterns is a fundamental aspect of mathematics, especially in algebra and arithmetic. Sequences provide a systematic way of listing numbers that follow specific rules, and finding particular terms within these sequences is a common problem in mathematical analysis. In this article, we will explore how to find the 8th term in the sequence $-\frac{1}{2}, -1, -2, -4, \dots$, providing a detailed step-by-step explanation, insights into the sequence's pattern, and tips for solving similar problems efficiently.

Introduction to Sequences and Their Types

Before delving into the specific sequence, it's essential to understand what sequences are and the different types that exist.

What Is a Sequence?

A sequence is an ordered list of numbers arranged according to a specific rule or pattern. Each number in a sequence is called a term. The position of the term in the sequence is called its index or term number.

For example, in the sequence 2, 4, 6, 8, 10, the first term (a_1) is 2, the second term (a_2) is 4, and so on.

Types of Sequences

Sequences can be broadly classified into various types:

- Arithmetic Sequences: Where each term differs from the previous by a constant difference.
- Geometric Sequences: Where each term is multiplied by a constant ratio to get the next term.
- Other sequences: Such as quadratic sequences, Fibonacci sequences, etc.

The sequence we are analyzing falls into the category of geometric sequences, as we will see.

Analyzing the Given Sequence

Let's examine the sequence provided:

-1/2, -1, -2, -4, ...

Our goal is to find the 8th term, denoted as a_8 .

Identifying the Pattern

To understand the pattern, look at the sequence carefully:

- Term 1 (a_1): -1/2
- Term 2 (a_2): -1
- Term 3 (a_3): -2
- Term 4 (a_4): -4

Let's analyze the relation between consecutive terms:

- From a_1 to a_2 : -1/2 to -1
- From a_2 to a_3 : -1 to -2
- From a_3 to a_4 : -2 to -4

Now, observe the ratios:

- $a_2 / a_1 = (-1) / (-1/2) = 2$
- $a_3 / a_2 = (-2) / (-1) = 2$
- $a_4 / a_3 = (-4) / (-2) = 2$

This indicates that each term is obtained by multiplying the previous term by 2:

$$a_n = a_{n-1} \times 2$$

Therefore, the sequence is geometric with a common ratio (r) of 2.

Finding the First Term

The first term is given as $a_1 = -1/2$.

Formulating the General Term

Since it's a geometric sequence with a ratio $r = 2$ and first term $a_1 = -1/2$, the general formula for the n th term of a geometric sequence is:

$$a_n = a_1 \times r^{(n-1)}$$

Substituting the known values:

$$a_n = (-1/2) \times 2^{(n-1)}$$

Calculating the 8th Term

Now, to find the 8th term, substitute $n = 8$ into the formula:

$$a_8 = (-1/2) \times 2^{(8-1)}$$

$$a_8 = (-1/2) \times 2^7$$

Calculate 2^7 :

$$2^7 = 128$$

Now, multiply:

$$a_8 = (-1/2) \times 128 = -128 / 2 = -64$$

Therefore, the 8th term of the sequence is -64.

Step-by-Step Summary

1. Recognize the sequence pattern by analyzing ratios between consecutive terms.
2. Determine that the sequence is geometric with ratio $r = 2$.
3. Identify the first term $a_1 = -1/2$.
4. Use the general geometric sequence formula: $a_n = a_1 \times r^{(n-1)}$.
5. Substitute $n = 8$ to find a_8 .
6. Simplify the expression to obtain the value of the 8th term.

Additional Tips for Solving Similar Sequence Problems

- Always look for a pattern: Check ratios or differences between terms.
- Identify the type of sequence: Arithmetic, geometric, or other.
- Find the first term and common ratio: These are crucial for the formula.
- Write the general term: Use the formula for geometric or arithmetic sequences.
- Substitute the term number: Plug in the position to find the specific term.
- Simplify carefully: Be mindful of negative signs and fractional calculations.

Practice Problems to Reinforce Learning

To solidify understanding, try solving these similar problems:

1. Find the 10th term in the sequence 3, 6, 12, 24, ...
2. Determine the 5th term of the sequence $1/3, 1/6, 1/12, 1/24, \dots$

3. Identify the 6th term in the sequence -2, 4, -8, 16, ...

Each of these problems involves recognizing the pattern, formulating the general term, and calculating the specific term.

Conclusion

Finding specific terms within a sequence requires understanding the sequence's pattern and applying the appropriate formula. In the case of the sequence $-1/2, -1, -2, -4, \dots$, recognizing that it is geometric with a ratio of 2 allows us to derive the general term and compute the 8th term accurately. Mastery of these techniques enhances problem-solving skills in algebra and prepares students for more advanced mathematical concepts involving sequences and series.

Summary of key points:

- The sequence is geometric with ratio $r = 2$.
- First term $a_1 = -1/2$.
- General term: $a_n = (-1/2) \times 2^{(n-1)}$.
- 8th term: $a_8 = -64$.

By following these steps and understanding the underlying pattern, you can confidently analyze and solve sequence-related problems efficiently.

Frequently Asked Questions

What is the pattern in the sequence $-1/2, -1, -2, -4, \dots$?

The sequence appears to be multiplying the previous term by 2, starting from $-1/2$: $(-1/2) \times 2 = -1$, $(-1) \times 2 = -2$, $(-2) \times 2 = -4$, and so on.

How can I find the 8th term in the sequence?

Identify the pattern (multiplying by 2 each time), then continue multiplying the previous term by 2 repeatedly until you reach the 8th term.

What is the general formula for the n th term in this sequence?

Yes, the sequence is geometric with the first term $a_1 = -1/2$ and common ratio $r = 2$. The n th term is $a_n = a_1 \times r^{(n-1)}$, which simplifies to $a_n = (-1/2) \times 2^{(n-1)}$.

What is the value of the 8th term in the sequence?

Using the formula $a_n = (-1/2) \times 2^{(n-1)}$, the 8th term is $a_8 = (-1/2) \times 2^{(8-1)} = (-1/2) \times 2^7 = (-1/2) \times 128 = -64$.

Are there any other methods to find the 8th term besides the formula?

Yes, you can also generate the sequence step-by-step by multiplying each term by 2 until reaching the 8th term, but using the formula is more efficient.

What type of sequence is this, geometric or arithmetic?

This is a geometric sequence because each term is obtained by multiplying the previous term by a constant ratio (2).

Can I apply the same method to find further terms in similar sequences?

Absolutely. For any geometric sequence, identifying the first term and common ratio allows you to find any term using the general formula.

Additional Resources

Find The 8th Term In The Sequence $-1/2, -1, -2, -4, \dots$

Understanding how to find a specific term in a sequence is a fundamental skill in mathematics, especially in algebra and number theory. The sequence $-1/2, -1, -2, -4, \dots$ presents an intriguing pattern that invites analysis and exploration. This article provides an in-depth review of how to determine the 8th term in this sequence, breaking down the process into manageable steps, examining the pattern, deriving the general formula, and discussing related concepts.

Introduction to the Sequence

Before diving into the process of finding the 8th term, it's essential to understand the nature of the sequence itself. The sequence is:

$-1/2, -1, -2, -4, \dots$

At first glance, the sequence appears to be decreasing and perhaps exponential or geometric in nature. Recognizing such patterns is critical in sequence analysis, as it guides the method used to find specific terms.

Identifying the Pattern

Examining the Terms

Let's analyze the first few terms carefully:

Term Number (n)	Term (T _n)	Numerical Value
1	T ₁	-1/2
2	T ₂	-1
3	T ₃	-2
4	T ₄	-4

From these, we can observe the following:

- $T_1 = -1/2$
- $T_2 = -1$
- $T_3 = -2$
- $T_4 = -4$

Looking at the ratios between successive terms:

- $T_2 / T_1 = (-1) / (-1/2) = 2$
- $T_3 / T_2 = (-2) / (-1) = 2$
- $T_4 / T_3 = (-4) / (-2) = 2$

This indicates the sequence is geometric with a common ratio of 2, but notice that the signs are negative throughout.

Establishing the Pattern: Geometric Sequence

Recognizing the Geometric Pattern

Since the ratios between successive terms are constant at 2, and all terms are negative, the sequence can be modeled as a geometric sequence:

$$T_n = T_1 \times r^{n-1}$$

where:

- (T_1) is the first term,
- (r) is the common ratio.

From the first term,

$$T_1 = \frac{1}{2}$$

and the common ratio,

$$r = 2.$$

Thus, the general formula becomes:

$$T_n = \frac{1}{2} \times 2^{n-1}$$

or simplified as:

$$T_n = 2^{n-2}$$

Deriving the Formula for the nth Term

General Term Formula

Based on the pattern observed, the explicit formula for the nth term is:

$$T_n = \frac{1}{2} \times 2^{n-1}$$

This formula allows us to compute any term in the sequence directly, without needing to find previous terms.

Simplification

Notice that:

$$\frac{1}{2} \times 2^{n-1} = \frac{1}{2} \times 2^{n-1} = 2^{n-2}$$

because:

$$\frac{1}{2} \times 2^{n-1} = \frac{2^{n-1}}{2} = 2^{n-2}$$

Thus, the simplified formula for the sequence is:

$$T_n = 2^{n-2}$$

$$T_{\{n\}} = -2^{\{n-2\}}$$

\]

This is a more straightforward expression to use for calculations.

Calculating the 8th Term

Applying the Formula

Using the simplified formula:

\[

$$T_{\{n\}} = -2^{\{n-2\}}$$

\]

we substitute \((n = 8 \) \):

\[

$$T_{\{8\}} = -2^{\{8-2\}} = -2^{\{6\}} = -64$$

\]

Therefore, the 8th term in the sequence is -64.

Verification of the Pattern

To ensure accuracy, let's verify other terms:

- For \((n=1 \) \):

\[

$$T_{\{1\}} = -2^{\{1-2\}} = -2^{\{-1\}} = -\frac{1}{2}$$

\]

which matches the first term.

- For \((n=2 \) \):

\[

$$T_{\{2\}} = -2^{\{2-2\}} = -2^{\{0\}} = -1$$

\]

matches the second term.

- For $(n=3)$:

$$T_{\{3\}} = -2^{\{3-2\}} = -2^{\{1\}} = -2$$

matches the third term.

- For $(n=4)$:

$$T_{\{4\}} = -2^{\{4-2\}} = -2^{\{2\}} = -4$$

matches the fourth term.

The pattern holds, confirming the formula's correctness.

Features and Characteristics of the Sequence

Features

- Geometric progression: The sequence is geometric with a ratio of 2.
- Exponential growth in magnitude: The absolute value of the terms doubles each time.
- Negative terms: The sequence consists entirely of negative numbers.
- Pattern recognition: Easily expressed with a simple formula, facilitating quick term calculations.

Pros

- Predictability: With the formula, any term can be computed directly.
- Simplicity: The sequence's pattern simplifies calculations and analysis.
- Educational value: Demonstrates geometric sequences and exponential functions.

Cons

- Limited to specific patterns: The formula applies specifically to this geometric sequence; irregular sequences require different methods.
- Sign pattern: The negative signs could cause confusion if not carefully accounted for in

calculations.

Related Concepts and Applications

Understanding Geometric Sequences

This sequence exemplifies geometric progression properties, which are widely applicable in finance (compound interest), population growth models, and radioactive decay.

Sequence Generalizations

- Variations with different initial terms or ratios can be explored for diverse applications.
- Recognizing patterns helps in solving more complex problems involving sequences and series.

Practical Applications

- Computer Science: Algorithm analysis often involves geometric sequences.
- Physics: Modeling exponential decay or growth processes.
- Economics: Compound interest calculations.

Conclusion

Finding the 8th term in the sequence $-1/2, -1, -2, -4, \dots$ involves recognizing the pattern as a geometric progression with a common ratio of 2. Deriving the general term formula:

$$\begin{aligned} & \backslash \\ T_n &= -2^{n-2} \\ & \backslash \end{aligned}$$

allows for straightforward computation, leading to the conclusion that the 8th term is -64. Understanding this process not only provides the specific answer but also reinforces key mathematical concepts related to sequences, exponential functions, and pattern recognition. Such skills are fundamental in various fields and serve as a powerful tool in problem-solving and analytical reasoning.

Summary of Key Points:

- The sequence is geometric with first term $(-\frac{1}{2})$ and ratio 2.
- The explicit formula for the n th term is $(T_n = -2^{n-2})$.
- The 8th term is (-64) .
- Recognizing patterns simplifies complex calculations and aids in understanding sequence behavior.

By mastering this approach, learners can confidently analyze similar sequences and apply their knowledge to diverse mathematical and real-world problems.

Find The 8th Term In The Sequence 1 2 1 2 4

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