

Consider A Relation $R(A, B, C, D, E, G, H, I, J)$ And Its FD Set $F = \{A \rightarrow BC, CD \rightarrow AE, E \rightarrow CHI, HJ\}$. 1) Check

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Understanding the design and integrity of relational databases is essential for efficient data management. In this article, we explore the relation $R(A, B, C, D, E, G, H, I, J)$ and its functional dependency (FD) set $F = \{A \rightarrow BC, CD \rightarrow AE, E \rightarrow CHI, HJ\}$. We will analyze this relation thoroughly, focusing on key concepts such as functional dependencies, candidate keys, normalization, and how to verify the properties of the relation based on the given FDs. This comprehensive review aims to enhance your understanding of relational database theory, optimize database design, and ensure data integrity.

Understanding the Relation R and Its Functional Dependencies

Relation R Overview

The relation R includes the attributes:

- A
- B
- C
- D
- E
- G
- H
- I
- J

These attributes form the basis of our analysis. The primary goal is to determine how these attributes relate to each other via the set of functional dependencies F.

Functional Dependency Set F

The set F contains the following dependencies:

- $A \rightarrow BC$
- $CD \rightarrow AE$
- $E \rightarrow CHI$
- HJ

Each dependency indicates how certain attributes determine others within the relation:

- $A \rightarrow BC$ means attribute A functionally determines B and C.
- $CD \rightarrow AE$ means the combination of C and D determines A and E.
- $E \rightarrow CHI$ indicates attribute E determines C, H, and I.
- HJ is a bit ambiguous, but in typical FD notation, it might be shorthand for a dependency involving H and J. Since no arrow is specified, it could be a typo or an incomplete dependency. For the purpose of this analysis, we'll interpret it as $H \rightarrow J$, assuming H determines J, which is a common pattern.

Understanding these dependencies allows us to analyze key attributes, candidate keys, normalization levels, and potential data anomalies.

Analyzing Functional Dependencies and Attribute Closures

Attribute Closure Concepts

The attribute closure of a set of attributes X (denoted as X^+) is the set of all attributes functionally determined by X using the set of FDs F.

Calculating closures helps identify candidate keys and assess normalization.

Calculating Attribute Closures

Let's compute some attribute closures to understand the dependencies:

1. Closure of A (A^+):

- Start with A.
- $A \rightarrow BC$, so add B and C.
- Now, $A^+ = \{A, B, C\}$.
- Check if other dependencies can be applied:
- C alone doesn't determine anything further.
- No other dependencies can be applied directly.
- Result: $A^+ = \{A, B, C\}$

2. Closure of C and D (CD^+):

- Start with C, D.
- $CD \rightarrow AE$, so add A and E.
- Now, $CD^+ = \{A, C, D, E\}$
- $E \rightarrow CHI$, so add C, H, I.
- E is already in the set, so add H and I.
- Now, $CD^+ = \{A, C, D, E, H, I\}$
- Check for further dependencies:
- HJ (assuming $H \rightarrow J$), so add J.
- Final closure: $CD^+ = \{A, C, D, E, H, I, J\}$

3. Closure of E (E^+):

- Start with E.
- $E \rightarrow CHI$, so add C, H, I.
- No other dependencies from these attributes directly.
- Result: $E^+ = \{E, C, H, I\}$

4. Closure of H (H^+):

- H alone does not determine anything unless $H \rightarrow J$ is assumed.
- Assuming $H \rightarrow J$:
- $H^+ = \{H, J\}$
- If no, then $H^+ = \{H\}$.

These closures help identify candidate keys and the minimal attribute sets that determine all other attributes.

Identifying Candidate Keys

Definition of Candidate Keys

A candidate key is a minimal set of attributes that functionally determines all attributes in the relation. Finding candidate keys involves analyzing attribute closures.

Candidate Keys in R

Let's analyze possible candidate keys based on the closures:

- Using A:
- $A^+ = \{A, B, C\}$
- B and C are determined, but D, E, G, H, I, J are not.
- So, A alone is not a candidate key.

- Using CD:
- $CD^+ = \{A, C, D, E, H, I, J\}$
- Missing B, G.
- To include B, note that $A \rightarrow BC$, so if A is included, B and C are determined.
- But since CD + includes A, perhaps CD is part of the key.

- Using C and D:
- $CD^+ = \{A, C, D, E, H, I, J\}$
- Missing B and G.
- G is not determined by any FD in F explicitly, so G might be part of the candidate key.

- Including G:
- G is not on the right side of any FD, so unless G is part of some

dependency, it remains undetermined.

- Including H and J:
- H J (assuming $H \rightarrow J$), starting with H, closure is {H, J}.
- To determine all attributes, more attributes are needed.

Conclusion:

- Candidate keys are likely to include A combined with other attributes to cover all attributes.
- A possible candidate key is A, D, G, or A, C, D, G, depending on the dependencies.

Note: Precise candidate key identification requires exhaustive closure calculations, but the above provides an overview.

Normalization and Data Integrity Considerations

Understanding Normal Forms

Normalization is the process of organizing data to reduce redundancy and improve data integrity. The common forms include:

1. First Normal Form (1NF): Atomicity of data.
2. Second Normal Form (2NF): No partial dependency on a candidate key.
3. Third Normal Form (3NF): No transitive dependencies.
4. Boyce-Codd Normal Form (BCNF): Every determinant is a candidate key.

Assessing R for Normalization

Based on the dependencies:

- The FD $A \rightarrow BC$ suggests that A determines B and C, which might indicate partial dependencies if A is part of a candidate key.
- The FD $CD \rightarrow AE$ indicates a dependency that involves a composite key.

To achieve higher normalization levels:

- Remove partial dependencies (achieving 2NF).
- Remove transitive dependencies (achieving 3NF).
- Ensure all determinants are candidate keys (achieving BCNF).

Example:

If A is part of a candidate key, then the dependency $A \rightarrow BC$ indicates a partial dependency, which violates 2NF. To normalize, one might decompose R into smaller relations.

Decomposition Strategies for R Based on FDs

Why Decompose?

Decomposition helps eliminate anomalies caused by functional dependencies, ensuring better data integrity, easier maintenance, and optimized queries.

Steps for Decomposition

1. Identify violations of normal forms.
2. Create relations that preserve dependencies.
3. Ensure lossless join and dependency preservation.

Sample Decomposition

- Relation $R_1(A, B, C)$: Based on $A \rightarrow BC$.
- Relation $R_2(C, D, A, E)$: Based on $CD \rightarrow AE$.
- Relation $R_3(E, C, H, I)$: Based on $E \rightarrow CHI$.
- Relation $R_4(H, J)$: Based on $H \rightarrow J$.

Each relation preserves a subset of dependencies and reduces redundancy.

Conclusion: Ensuring Data Integrity in Relation R

Understanding and analyzing functional dependencies in relation $R(A, B, C, D, E, G, H, I, J)$ is crucial for designing a robust database schema. By calculating attribute closures, identifying candidate keys, and applying normalization principles, database designers can eliminate redundancy and ensure data consistency.

Proper decomposition based on FDs enhances data integrity, simplifies maintenance, and optimizes query performance. While the process involves detailed calculations, mastering these concepts enables you to create efficient, reliable relational databases.

Key Takeaways:

- Functional dependencies define how attributes relate within a relation.
- Attribute closures help identify candidate keys.
- Normalization reduces redundancy and prevents anomalies.
- Decomposition based on FDs preserves data integrity.

By applying these principles, you can improve your database design process, ensuring your relational schema is both efficient and reliable.

SEO Keywords: relational database design, functional dependencies, candidate keys, normalization, database normalization, attribute closure, data integrity, database decomposition, BCNF, 1NF, 2NF, 3NF, relational schema optimization

Frequently Asked Questions

Given the relation $R(A, B, C, D, E, G, H, I, J)$ with the functional dependencies $F = \{AB \rightarrow C, CD \rightarrow AE, E \rightarrow CHI, HJ\}$, how do you determine if R is in 3NF?

To check if R is in 3NF, verify that for every FD $X \rightarrow Y$, either X is a superkey or Y is a prime attribute. First, find candidate keys; then, ensure no non-prime attribute depends on a non-key attribute. If these conditions hold, R is in 3NF.

How do you compute the candidate key(s) for relation R based on the given FD set F ?

Start by identifying the attributes that determine all others. For example, since $AB \rightarrow C$, and $CD \rightarrow AE$, and $E \rightarrow CHI$, HJ is also given, you can derive attribute closures to find minimal sets that functionally determine all attributes. The candidate key could be AB and possibly other minimal combinations found through closure calculations.

What is the process to decompose R into Boyce-Codd Normal Form (BCNF) using the given FD set?

Identify any FD that violates BCNF, i.e., where the determinant is not a superkey. Then, decompose R into relations where each relation's key is a candidate key, ensuring all FDs are preserved or their projections are. Repeat this process until all relations are in BCNF.

Are there any partial dependencies in R with respect to its candidate key(s), and how do they affect normalization?

Partial dependencies occur when a non-prime attribute depends on part of a candidate key. By analyzing the FDs, check if any attribute depends on a subset of a candidate key. If such dependencies exist, the relation is not in 2NF and requires decomposition to remove partial dependencies for higher normal forms.

How do the given functional dependencies influence the design of a normalized schema for R?

The FDs guide the identification of keys, candidate keys, and normalization steps. They help detect redundancies, partial, and transitive dependencies, enabling the design of a schema that minimizes anomalies by decomposing R into well-structured relations that adhere to normal forms.

Additional Resources

In-depth Analysis and Evaluation of the Relation $R(A, B, C, D, E, G, H, I, J)$ and Its Functional Dependency Set F

Introduction

Understanding the properties and structure of a relation within the context of relational databases is foundational to designing efficient and normalized database schemas. The relation $R(A, B, C, D, E, G, H, I, J)$, accompanied by the set of functional dependencies $F = \{A \rightarrow BC, CD \rightarrow AE, E \rightarrow CHI, HJ\}$, presents an interesting case for analysis. This review delves into the core aspects of this relation and its functional dependencies, examining their implications for normalization, keys, closure computations, and overall database design integrity.

1. Basic Understanding of the Relation and Functional Dependencies

1.1 Relation Schema Overview

The relation R contains the attributes:

- $A, B, C, D, E, G, H, I, J$

Total attributes: 9

The primary goal is to analyze how these attributes are functionally related, identify candidate keys, assess normalization levels, and understand the potential anomalies that might occur if the relation is not properly normalized.

1.2 Functional Dependency Set F

The set F consists of four functional dependencies:

- $A \rightarrow BC$
- $CD \rightarrow AE$

3. $E \rightarrow CHI$

4. HJ

Each of these dependencies constrains the attribute relationships within R and guides the normalization process.

2. Analyzing the Functional Dependencies

2.1 Breakdown of Each Dependency

- $A \rightarrow BC$: The attribute A functionally determines B and C. This indicates that knowing A allows us to uniquely identify B and C.

- $CD \rightarrow AE$: The combination of C and D determines A and E. This suggests a composite determinant, possibly hinting at candidate key components.

- $E \rightarrow CHI$: E determines C, H, and I. This indicates a transitive dependency where E influences multiple attributes.

- HJ: This dependency is somewhat ambiguous as it lacks an arrow, but assuming it's a typo and should be interpreted as $H \rightarrow J$, it indicates H determines J.

Note: The last dependency, HJ, appears incomplete; typically, a dependency involves an arrow. It's likely meant to be $H \rightarrow J$. For clarity, we proceed with this assumption.

2.2 Implications of Dependencies

- $A \rightarrow BC$: A is a candidate key or part of one since it determines B and C, which are attributes of R.

- $CD \rightarrow AE$: The combination of C and D influences A and E, potentially creating composite keys or partial keys.

- $E \rightarrow CHI$: E's influence on C, H, and I suggests that E is a determinant for multiple attributes, possibly indicating that E is a candidate key or part of one.

- $H \rightarrow J$: H determines J, establishing a direct dependency that helps in understanding attribute hierarchy.

3. Closure Computations and Candidate Keys

Understanding the candidate keys requires computing attribute closures based on the FD set $\mathcal{F}$.

3.1 Computing Attribute Closures

To identify candidate keys, we compute the attribute closure for different attribute combinations.

Note: We only include relevant dependencies in each closure calculation.

3.1.1 Closure of A: A^+

- Start with A: $A^+ = \{A\}$
- From $A \rightarrow BC$: $A^+ = \{A, B, C\}$
- No other dependencies apply directly with current closure.
- Result: $A^+ = \{A, B, C\}$

Conclusion: A alone doesn't determine all attributes; thus, A is not a candidate key.

3.1.2 Closure of E: E^+

- Start with E: $E^+ = \{E\}$
- From $E \rightarrow CHI$: $E^+ = \{E, C, H, I\}$
- Now, check if any other dependencies apply:
- $A \rightarrow BC$: no, since we don't have A in the closure.
- $CD \rightarrow AE$: need C and D, but C is in the closure, D is not.
- $H \rightarrow J$: H is in the closure, so J can be added.
- Adding J: $E^+ = \{E, C, H, I, J\}$
- Now, check if any other dependencies are applicable:
- $CD \rightarrow AE$: C is in the closure; D is not, so can't proceed without D.
- Is D in the closure? No.
- Result: $E^+ = \{E, C, H, I, J\}$
- Attributes covered: E, C, H, I, J.
- Remaining attributes: A, B, D, G remain outside the closure.

3.1.3 Closure of C and D: $\overline{CD}$

- Start with C and D: $\{C, D\}$
- From $CD \rightarrow AE$: add A and E

$\{A, C, D, E\}$

- From $A \rightarrow BC$: A gives B (already in closure), C is known.
- From $E \rightarrow CHI$: E gives C (already known), H, I.

$\{A, B, C, D, E, H, I\}$

- Now, H gives J: add J.

$\{A, B, C, D, E, H, I, J\}$

- Remaining attributes: G is not in the closure.
- Result: $\overline{CD} = \{A, B, C, D, E, H, I, J\}$
- Attributes left unaccounted: G.

Observation: The closure of $\{C, D\}$ includes all attributes except G, indicating that $\{C, D\}$ is a candidate key for R minus G.

3.1.4 Closure of H: $\overline{H}$

- Start: $\{H\}$
- From $H \rightarrow J$: add J.
- $\overline{H} = \{H, J\}$
- No other dependencies apply.
- Attributes remaining: A, B, C, D, E, G, I are outside the closure.

3.1.5 Closure of other attribute combinations

Similarly, other combinations such as $\{A, E, H\}$, or $\{A, C, D\}$, can be checked to identify candidate keys.

4. Candidate Key Identification

Based on the closure computations, candidate keys are minimal attribute sets that determine all attributes in R.

4.1 Candidate Key 1: $\{C, D\}$

- As previously computed, $\{C, D\}^+ = \{A, B, C, D, E, H, I, J\}$
- Missing attribute: G
- Conclusion: $\{C, D\}$ is not a candidate key for the entire relation R, unless G is dependent on $\{C, D\}$, which it isn't based on current dependencies.

4.2 Candidate Key 2: $\{C, D, G\}$?

- Since $\{C, D\}$ covers all attributes except G, including G in the key would make it a candidate key.
- Check the closure of $\{C, D, G\}$:
- Already, $\{C, D\}$ gives all attributes except G, so adding G makes it complete.
- Result: $\{C, D, G\}$ is a candidate key.

4.3 Candidate Key 3: $\{E, G\}$?

- $\{E\}^+$ includes $\{E, C, H, I, J\}$, but not A, B, D, G.
- Adding G: $\{E, G\}$
- Check if this set determines all attributes.
- From $\{E\} \rightarrow C, H, I$, attributes are covered.
- G is included.
- Does $\{E, G\}$ determine A, B, D?
- To determine A: analyze dependencies.
- $\{C, D\} \rightarrow A, E$: needs C and D; no.
- No dependencies directly link $\{E, G\}$ to D or A.
- So, $\{E, G\}$ is not a candidate key unless combined with other attributes.

5. Normalization Analysis

Normalization aims to eliminate redundancy and anomalies. We examine the relation R with respect to the set $\mathcal{F}$ to identify its highest normal form.

5.1 First Normal Form (1NF)

- R is in 1NF by default, assuming atomic attributes.

5.2 Second Normal Form (2NF)

- Requires that there are no partial dependencies of non-prime attributes on a part of a candidate key.
- Based on the candidate key $\{C, D, G\}$, dependencies such as $\{A \rightarrow BC\}$ and $\{E \rightarrow CHI\}$ are not partial dependencies, as A and E are not part of the candidate key.
- No partial dependencies are evident; R may be in 2NF.

5.3 Third Normal Form (3NF)

- For

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