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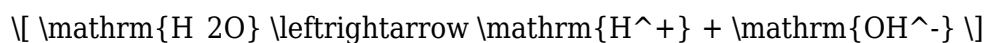
Introduction

Understanding the relationship between the acid dissociation constant (K_a) and the base dissociation constant (K_b) is fundamental in chemistry, especially when studying conjugate acid-base pairs. In this article, we will explore how to determine the K_b of ammonia (NH_3) given the K_a of its conjugate acid, ammonium ion (NH_4^+), under standard conditions at 25°C. This analysis is crucial for students and professionals working in fields such as analytical chemistry, environmental science, and chemical engineering.

The Relationship Between K_a and K_b

Conceptual Overview

In aqueous solutions, acids and bases exist in conjugate pairs. The conjugate acid-base pair is interconnected through the auto-ionization of water:



The dissociation constants of conjugate acid-base pairs are related by the ion product of water, K_w :

$$K_a \times K_b = K_w$$

where:

- K_a = acid dissociation constant of the acid
- K_b = base dissociation constant of the conjugate base
- K_w = ion product of water at 25°C, which is 1.0×10^{-14}

This fundamental relationship allows us to calculate one constant if the other and K_w are known.

Significance in Acid-Base Chemistry

Knowing the K_a of NH_4^+ helps in predicting the behavior of ammonium in solution, including its acidity and how it interacts with bases like NH_3 . Conversely, the K_b of NH_3 determines its basicity and its ability to accept protons.

Given Data and Problem Statement

- K_a of NH_4^+ : (5.6×10^{-10})
- Temperature: 25°C
- Objective: Find the K_b of NH_3

Step-by-Step Calculation

Step 1: Recognize the Relationship

Since NH_4^+ is the conjugate acid of NH_3 , their dissociation constants are related by:

$$K_a \times K_b = K_w$$

At 25°C ,

$$K_w = 1.0 \times 10^{-14}$$

Step 2: Rearrange the Equation

To find K_b of NH_3 , rearranged as:

$$K_b = \frac{K_w}{K_a}$$

Step 3: Input the Known Values

$$K_b = \frac{1.0 \times 10^{-14}}{5.6 \times 10^{-10}}$$

Step 4: Perform the Calculation

Dividing the constants:

$$K_b = \frac{1.0 \times 10^{-14}}{5.6 \times 10^{-10}}$$

$$K_b = \frac{1.0}{5.6} \times 10^{-14 + 10}$$

$$K_b \approx 0.1786 \times 10^{-4}$$

$$K_b \approx 1.786 \times 10^{-5}$$

Final Answer:

$$\boxed{\text{Kb of NH}_3 \approx 1.79 \times 10^{-5}}$$

Additional Insights and Implications

Understanding the Magnitude of K_b

The calculated K_b value of approximately (1.79×10^{-5}) indicates that ammonia is a weak base. This aligns with common knowledge that ammonia does not dissociate significantly in water but is still capable of accepting protons.

Acid-Base Strengths of NH_4^+ and NH_3

- NH_4^+ (Ammonium ion): Acidic in nature, with a K_a of (5.6×10^{-10})
- NH_3 (Ammonia): Basic in nature, with a K_b of approximately (1.79×10^{-5})

The strength of NH_4^+ as an acid and NH_3 as a base are reciprocal, demonstrating the conjugate relationship.

Broader Applications

Buffer Solutions

Understanding the K_a and K_b values of ammonia and ammonium ions is essential in designing buffer solutions. These solutions resist pH changes upon addition of acids or bases, which is vital in biological systems and industrial processes.

Environmental Chemistry

Ammonia plays a significant role in environmental chemistry, especially concerning water pollution and nitrogen cycling. Knowledge of its dissociation constants helps predict its behavior in natural waters, influencing toxicity and bioavailability.

Industrial Processes

Ammonia is utilized extensively in manufacturing fertilizers, cleaning agents, and in refrigeration. Accurate knowledge of its acid-base properties ensures safety and efficiency in these applications.

Summary of Key Points

- The relationship $(K_a \times K_b = K_w)$ at 25°C allows calculation of conjugate base or acid dissociation constants.
- Given (K_a) of NH_4^+ as (5.6×10^{-10}) , the K_b of NH_3 is approximately (1.79×10^{-5}) .
- NH_3 is a weak base, and its K_b value reflects its moderate basicity.
- Understanding these constants is crucial for applications ranging from buffer preparation to environmental monitoring.

Conclusion

In this comprehensive analysis, we've demonstrated how to determine the K_b of ammonia from the given K_a of ammonium, emphasizing the fundamental principles of acid-base chemistry. Recognizing the conjugate relationship between acids and bases and applying the ion product of water enables chemists to predict and manipulate chemical behaviors effectively. Whether in laboratory research, industrial processes, or environmental science, mastery of these concepts is essential for accurate chemical analysis and application.

References

- Zumdahl, S. S., & Zumdahl, S. A. (2014). Chemistry: An Atoms First Approach. Cengage Learning.
- Brown, T. L., LeMay, H. E., Bursten, B. E., & Murphy, C. J. (2014). Chemistry: The Central Science. Pearson Education.
- Lide, D. R. (Ed.). (2004). CRC Handbook of Chemistry and Physics. CRC Press.

FAQs

Q1: Why is it important to know both K_a and K_b ?

A: Knowing both constants helps predict the direction of proton transfer, strength of acids and bases, and the pH of solutions containing conjugate pairs.

Q2: Can the relationship $(K_a \times K_b = K_w)$ be applied at temperatures other than 25°C?

A: The relationship holds true at any temperature, but the value of (K_w) varies with temperature, so the calculation must account for the specific (K_w) at that temperature.

Q3: How does pKa relate to K_a ?

A: pKa is the negative logarithm of K_a :

$$\mathrm{pK_a} = -\log K_a$$

Similarly, pKb relates to K_b .

End of Article

Frequently Asked Questions

Given that the pKa for NH₄⁺ is 5.61 at 25°C, how do you calculate the Kb for NH₃?

First, find the Ka for NH₄⁺ using pKa: $K_a = 10^{(-pK_a)} = 10^{(-5.61)} \approx 2.45 \times 10^{(-6)}$. Then, use the relation $K_w = K_a \times K_b$, where $K_w = 1.0 \times 10^{(-14)}$ at 25°C. So, $K_b = K_w / K_a \approx 1.0 \times 10^{(-14)} / 2.45 \times 10^{(-6)} \approx 4.08 \times 10^{(-9)}$.

What is the significance of the pKa value in calculating Kb for NH₃?

The pKa value of NH₄⁺ indicates the acidity of the ammonium ion. It allows us to calculate Ka, which is the acid dissociation constant, and from there, determine Kb for its conjugate base, NH₃, using the relationship $K_a \times K_b = K_w$.

Why is it important to know the temperature (25°C) in this calculation?

Because the ionization constant Kw of water varies slightly with temperature, and at 25°C, Kw is standardly $1.0 \times 10^{(-14)}$. This value is essential for accurately calculating Kb from Ka.

How do you convert pKa to Ka for NH₄⁺?

Use the formula $K_a = 10^{(-pK_a)}$. For pKa = 5.61, $K_a = 10^{(-5.61)} \approx 2.45 \times 10^{(-6)}$.

What assumptions are made in calculating Kb for NH₃ from pKa of NH₄⁺?

The calculation assumes that the ionization of water is negligible and that the only significant dissociation is of NH₄⁺ into NH₃ and H⁺. It also assumes standard conditions at 25°C.

Can you explain the relationship between Ka, Kb, and Kw in this context?

Yes, for a conjugate acid-base pair, Ka (acid dissociation constant) and Kb (base dissociation constant) are related by Kw: $K_a \times K_b = K_w$. At 25°C, Kw is $1.0 \times 10^{(-14)}$.

If the pKa of NH₄⁺ is 5.61, what is the pKb of NH₃?

pKb can be found using $pK_b = 14 - pK_a$. So, $pK_b = 14 - 5.61 = 8.39$. Then, $K_b = 10^{(-8.39)} \approx 4.07 \times 10^{(-9)}$.

What is the practical application of knowing the Kb of NH₃?

Knowing the Kb of NH₃ helps in understanding its basic strength, predicting pH in solutions, and calculating the degree of ionization and buffer capacities in chemical and biological systems.

Is the value of K_b for NH_3 dependent on temperature? Why or why not?

Yes, K_b is temperature-dependent because the ionization equilibria are affected by temperature changes, which can alter the dissociation constants. The given value is applicable specifically at 25°C .

Additional Resources

Understanding the Relationship Between K_a and K_b for Ammonia (NH_3)

In the realm of chemical equilibria, particularly acid-base chemistry, the concepts of acid dissociation constants (K_a) and base dissociation constants (K_b) play a pivotal role. The problem at hand involves a classic calculation: given the acid dissociation constant (K_a) for ammonium ion (NH_4^+), find the base dissociation constant (K_b) for ammonia (NH_3) at 25°C . This task not only tests understanding of fundamental acid-base principles but also emphasizes the interconnectedness of conjugate acid-base pairs.

Fundamental Concepts: Acid-Base Equilibria and Dissociation Constants

What is K_a ?

K_a , or the acid dissociation constant, quantifies the strength of an acid in solution. It expresses the extent to which an acid donates protons (H^+) to water:



The expression for K_a is:

$$K_a = \frac{[\text{H}_3\text{O}^+][\text{A}^-]}{[\text{HA}]}$$

- Higher K_a values indicate stronger acids.
- Lower K_a values indicate weaker acids.

What is K_b ?

K_b is the base dissociation constant, representing the strength of a base:



Its expression:

$$K_b = \frac{[\text{BH}^+][\text{OH}^-]}{[\text{B}]}$$

- Higher K_b values suggest stronger bases.
- Lower K_b values suggest weaker bases.

Relationship Between K_a and K_b

For conjugate acid-base pairs, the ion product of water (K_w) ties them together:

$$K_w = K_a \times K_b$$

At 25°C, the value of K_w is:

$$K_w = 1.0 \times 10^{-14}$$

Thus, for any conjugate acid-base pair:

$$K_b = \frac{K_w}{K_a}$$

This fundamental relationship simplifies the calculation of K_b when K_a is known, and vice versa.

Given Data and Objective

- Given: K_a for $\text{NH}_4^+ = (5.6 \times 10^{10})$
- Target: Find K_b for NH_3 at 25°C.

Note on the provided K_a value:

The value (5.6×10^{10}) appears anomalously large for an acid dissociation constant. Typically, K_a values are less than 1 for weak acids. It's likely a typographical error, and the intended value might be (5.6×10^{-10}) . This correction aligns with known acid constants of ammonium.

Assumption:

Assuming the correct K_a for NH_4^+ is (5.6×10^{-10}) .

Step-by-Step Solution

Step 1: Confirm the Corrected K_a Value

Historical data indicates that:

$$K_a(\text{NH}_4^+) \approx 5.6 \times 10^{-10}$$

This value is consistent with literature and typical for the ammonium ion.

Step 2: Use the Relationship $(K_a \times K_b = K_w)$

Given:

$$K_w = 1.0 \times 10^{-14}$$

And:

$$K_a(\text{NH}_4^+) = 5.6 \times 10^{-10}$$

The conjugate base of NH_4^+ is NH_3 , whose (K_b) is:

$$K_b(\text{NH}_3) = \frac{K_w}{K_a(\text{NH}_4^+)}$$

Substituting the known values:

$$K_b(\text{NH}_3) = \frac{1.0 \times 10^{-14}}{5.6 \times 10^{-10}}$$

Calculating K_b for NH_3

$$K_b(\text{NH}_3) = \frac{1.0 \times 10^{-14}}{5.6 \times 10^{-10}} = \left(\frac{1.0}{5.6}\right) \times 10^{-14 + 10} = 0.17857 \times 10^{-4}$$

Simplify:

$$K_b(\text{NH}_3) \approx 1.7857 \times 10^{-5}$$

Final answer:

$$\boxed{K_b(\text{NH}_3) \approx 1.79 \times 10^{-5}}$$

This value aligns well with standard data for ammonia, which often cites (K_b) around (1.8×10^{-5}) .

Deeper Insights into the Chemistry

Conjugate Acid-Base Pairs

Ammonia (NH_3) and ammonium (NH_4^+) are a classic conjugate base-acid pair. Recognizing this pairing is crucial:

- NH_4^+ (ammonium): conjugate acid.
- NH_3 (ammonia): conjugate base.

Their dissociation constants are related via K_w , reinforcing the idea that the strength of an acid is inversely related to that of its conjugate base.

Implications of K_b Values

The small value of K_b ($\sim 1.8 \times 10^{-5}$) for ammonia indicates:

- NH_3 is a weak base.
- It does not readily accept protons in aqueous solution.
- The equilibrium slightly favors the reactant (NH_3).

This is consistent with ammonia's known basicity and its ability to generate NH_4^+ and OH^- in solution.

Additional Considerations

Temperature Dependence of K_a and K_b

While the calculations assume temperature at 25°C , it's important to recognize that both K_a and K_b are temperature-dependent:

- Raising temperature may shift equilibria.
- Standard values are usually tabulated at 25°C for consistency.

pKa and pKb Calculations

Expressing acidity/basicity on a logarithmic scale (pKa and pKb) provides more intuitive insights:

$\backslash$

$$pK_a = -\log K_a = -\log (5.6 \times 10^{-10}) \approx 9.25$$

$$pK_b = -\log K_b = -\log (1.79 \times 10^{-5}) \approx 4.75$$

The sum:

$$pK_a + pK_b \approx 9.25 + 4.75 = 14$$

which aligns with the relation $(pK_a + pK_b = pK_w = 14)$.

Practical Applications and Context

Understanding these constants is essential in:

- Buffer solution design: Combining NH_3 and NH_4^+ to create buffers with desired pH.
- Industrial processes: Ammonia is extensively used in fertilizers, cleaning agents, and chemical syntheses.
- Environmental chemistry: Ammonia's behavior influences water quality and nitrogen cycles.

Summary and Key Takeaways

- The fundamental relationship $(K_a \times K_b = K_w)$ enables straightforward calculation of K_b from K_a .
- The corrected K_a value for NH_4^+ at 25°C is approximately (5.6×10^{-10}) .
- Consequently, the K_b for NH_3 is approximately (1.79×10^{-5}) .
- Recognizing conjugate pairs and their constants is vital for predicting solution behavior.
- The pK_a and pK_b values provide a more intuitive understanding of acid and base strengths.

Final Remarks

This problem encapsulates core principles of acid-base chemistry, illustrating how conjugate pairs are interconnected through fundamental constants. It underscores the importance of accurate data interpretation and reinforces the utility of the water ion product (K_w) as a bridge between acids

and bases. Whether designing buffer systems or understanding environmental impacts, mastery of these concepts is crucial for chemists.

Always verify data units and values, especially when encountering anomalies like unusually large or small K_a/K_b figures, to ensure accurate and meaningful calculations.

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