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Understanding the distribution of chairs in a school hall is an interesting exercise in fractions, ratios, and basic arithmetic. When given a scenario where a certain proportion of chairs are red, blue, and yellow, it becomes essential to analyze the problem systematically to find out the total number of chairs and how they are distributed among the different colors. This article explores this problem in detail, providing insights into how to approach such fraction-based questions, and demonstrating step-by-step calculations to arrive at the solution.

Breaking Down the Problem

The problem states that:

- $\frac{2}{5}$ of the chairs are red
- $\frac{3}{7}$ of the chairs are blue
- The remaining chairs are yellow
- There are 24 yellow chairs

Using this information, our goal is to determine:

- The total number of chairs in the hall
- The number of red and blue chairs

Understanding Fractions and Their Role

Fractions are a way to represent parts of a whole. In this context:

- $\frac{2}{5}$ indicates that two parts out of five are red chairs
- $\frac{3}{7}$ indicates that three parts out of seven are blue chairs
- The rest are yellow chairs

Since the total number of chairs is divided among these categories, and the remaining chairs are yellow, we can set up equations to find the total.

Step-by-Step Solution Strategy

To solve the problem, follow these steps:

Step 1: Assign a Variable for Total Chairs

Let the total number of chairs in the hall be denoted by T.

Step 2: Express the Number of Red and Blue Chairs

- Number of red chairs = $(\frac{2}{5}) T$
- Number of blue chairs = $(\frac{3}{7}) T$

Step 3: Express the Number of Yellow Chairs

- Since the rest are yellow, number of yellow chairs = $T - (\text{red} + \text{blue})$

Given that the number of yellow chairs is 24, we have:

$$\text{Number of yellow chairs} = 24$$

So:

$$T - [(\frac{2}{5}) T + (\frac{3}{7}) T] = 24$$

Calculating the Total Number of Chairs

Now, solve the equation to find T.

Step 4: Combine the Fractions

Find a common denominator for the fractions $(\frac{2}{5})$ and $(\frac{3}{7})$:

- Denominator 5 and 7 have a common denominator of 35.

Express the fractions with denominator 35:

$$- (2/5) = (2 \cdot 7)/(5 \cdot 7) = 14/35$$

$$- (3/7) = (3 \cdot 5)/(7 \cdot 5) = 15/35$$

Now, write the equation:

$$T - [(14/35) T + (15/35) T] = 24$$

Combine the fractions:

$$T - [(14/35 + 15/35) T] = 24$$

Simplify:

$$T - (29/35) T = 24$$

Step 5: Simplify and Solve for T

Express T as a common factor:

$$T (1 - 29/35) = 24$$

Calculate:

$$1 - 29/35 = (35/35) - (29/35) = 6/35$$

So:

$$T (6/35) = 24$$

Multiply both sides by 35/6 to isolate T:

$$T = 24 (35/6)$$

Simplify:

First, divide 24 by 6:

$$24 / 6 = 4$$

Then multiply:

$$T = 4 \cdot 35 = 140$$

Total number of chairs in the hall = 140

Determining the Number of Chairs of Each Color

Now that we know $T = 140$, calculate the number of red, blue, and yellow chairs.

Red Chairs

$$\text{Number of red chairs} = \left(\frac{2}{5}\right) 140 = (2 \cdot 140)/5 = 280/5 = 56$$

Blue Chairs

$$\text{Number of blue chairs} = \left(\frac{3}{7}\right) 140 = (3 \cdot 140)/7 = 420/7 = 60$$

Yellow Chairs

$$\text{Number of yellow chairs} = T - (\text{red} + \text{blue}) = 140 - (56 + 60) = 140 - 116 = 24$$

This matches the given number of yellow chairs, confirming our calculations.

Summary of the Distribution

Chair Color	Quantity
Red	56
Blue	60
Yellow	24

$$\text{Total chairs} = 140$$

Practical Applications of Such Fraction Problems

Understanding how to handle fractional parts of a whole is vital in many real-world situations, including:

- Event Planning: Allocating seats or resources proportionally
- Budget Distribution: Dividing funds among departments
- Inventory Management: Distributing stock based on percentages
- Educational Contexts: Teaching students about ratios and fractions

Additional Tips for Solving Fraction Distribution Problems

- Always identify what the fractions represent and what the total is.
- Convert fractions to have a common denominator to combine them easily.
- Use algebraic equations to relate parts to the whole.
- Verify your solution by checking if the parts sum up to the total.

Conclusion

This problem offers a clear example of applying fractional reasoning and algebraic techniques to real-world scenarios. By systematically setting up the problem, converting fractions to a common denominator, and solving for the total, we determined that the school hall contains 140 chairs, with 56 red, 60 blue, and 24 yellow chairs. Mastery of such problems enhances mathematical reasoning and problem-solving skills, which are valuable in many academic and practical contexts.

FAQs

1. What is the significance of finding a common denominator?

It simplifies the addition or subtraction of fractions, making calculations more straightforward.

2. Can this method be used for other fractional distribution problems?

Yes, the approach is versatile and applies to any situation involving parts of a whole expressed as fractions.

3. How do I verify my answer?

Ensure that the sum of all parts equals the total quantity, and cross-check calculations for accuracy.

Frequently Asked Questions

How many chairs are red in the school hall?

There are 10 chairs that are red.

How many chairs are blue in the school hall?

There are 12 chairs that are blue.

What is the total number of chairs in the hall?

The total number of chairs is 46.

How many chairs are yellow in the hall?

There are 24 chairs that are yellow.

How do you find the total number of chairs based on the given fractions?

You sum the parts: red ($\frac{2}{5}$), blue ($\frac{3}{7}$), and yellow (rest). Using the given yellow chairs, you can find the total and then calculate red and blue chairs accordingly.

Are the given fractions of red and blue chairs consistent with the total chairs?

Yes, when calculated with the total of 46 chairs, the fractions for red ($\frac{2}{5}$) and blue ($\frac{3}{7}$) fit correctly with the given number of yellow chairs.

What is the process to verify the number of chairs of each color?

Calculate the total number of chairs, then find the number of red and blue chairs using their fractions, and verify that the remaining chairs match the given yellow count.

Additional Resources

Chairs in a School Hall: An Analytical Breakdown of Color Distribution and Quantitative Insights

Introduction: Understanding the Classroom Environment and Its Visual Dynamics

Design and arrangement within educational spaces are more than just logistical considerations—they influence the learning atmosphere, student engagement, and overall aesthetics. Among these elements, chairs play a pivotal role, serving both functional and visual purposes. The distribution of chair colors can reflect intentional design choices, resource allocation, or simply logistical necessities.

In this detailed analysis, we explore a hypothetical scenario: a school hall where $\frac{2}{5}$ of the chairs are red, $\frac{3}{7}$ are blue, and the rest are yellow, with 24 yellow chairs explicitly specified. This case offers an excellent opportunity to delve into fractional reasoning, proportional calculations, and real-world applications of mathematics in designing and understanding communal spaces.

Deciphering the Distribution: Breaking Down the Problem

The core challenge lies in determining the total number of chairs in the hall based on the given fractions and the explicit number of yellow chairs. Once the total is known, we can explore the distribution of red and blue chairs and analyze the proportionality and logical consistency within the scenario.

The Given Data:

- Fraction of red chairs: $\frac{2}{5}$
- Fraction of blue chairs: $\frac{3}{7}$
- Remaining chairs: Yellow
- Number of yellow chairs: 24

Mathematical Approach to the Problem

To understand the distribution, we need to establish a relationship between the fractions and the actual counts. The key steps involve:

1. Define the total number of chairs as (T) .
2. Express the number of yellow chairs in terms of (T) .

3. Use the known number of yellow chairs to find (T) .
4. Calculate the number of red and blue chairs based on (T) .

Step 1: Expressing the Number of Chairs in Terms of Total (T)

Let's denote:

- Number of red chairs = (R)
- Number of blue chairs = (B)
- Number of yellow chairs = (Y)

From the problem:

- $R = \frac{2}{5}T$
- $B = \frac{3}{7}T$
- $Y = T - R - B$

Since (Y) is explicitly given as 24, we can write:

$$Y = T - \frac{2}{5}T - \frac{3}{7}T = 24$$

Step 2: Formulating the Equation

Combining the fractions:

$$Y = T - \left(\frac{2}{5}T + \frac{3}{7}T \right) = 24$$

Expressing the sum inside parentheses with a common denominator:

$$\frac{2}{5}T + \frac{3}{7}T = \left(\frac{2 \times 7}{5 \times 7} + \frac{3 \times 5}{7 \times 5} \right) T = \left(\frac{14}{35} + \frac{15}{35} \right) T = \frac{29}{35} T$$

Substituting back:

$$Y = T - \frac{29}{35} T = 24$$

Simplify:

$$Y = \left(1 - \frac{29}{35} \right) T = 24$$

$$\left(\frac{35}{35} - \frac{29}{35} \right) T = 24$$

$$\frac{6}{35} T = 24$$

Step 3: Solving for (T)

Multiply both sides by $\left(\frac{35}{6} \right)$:

$$T = 24 \times \frac{35}{6}$$

Simplify:

$$T = 24 \times \frac{35}{6} = 24 \times \frac{35}{6}$$

Divide numerator and denominator:

$$T = 24 \times \frac{35}{6} = (24 \div 6) \times 35 = 4 \times 35 = 140$$

Therefore, the total number of chairs in the hall is 140.

Distribution of Chairs Based on Total Count

With $(T = 140)$:

- Red chairs: $(R = \frac{2}{5} \times 140 = 2 \times 28 = 56)$
- Blue chairs: $(B = \frac{3}{7} \times 140 = 3 \times 20 = 60)$
- Yellow chairs: $(Y = 24)$ (as given)

Check Total:

$$R + B + Y = 56 + 60 + 24 = 140$$

The distribution sums perfectly, confirming the consistency of our calculations.

Analyzing the Distribution and Its Implications

Now that the total count and distribution are established, let's delve into what this means in terms of visual appeal, resource allocation, and potential design considerations.

Visual Balance and Color Dominance

- Red Chairs (56): Approximately 40% of total chairs.
- Blue Chairs (60): About 43% of total chairs.
- Yellow Chairs (24): Constituting roughly 17%.

This distribution indicates a predominantly blue and red environment with relatively fewer yellow chairs, which could influence the hall's aesthetic or functional zoning (e.g., yellow chairs reserved for specific groups or purposes).

Resource Allocation and Procurement

Understanding these proportions aids in budgeting and procurement:

- Buying in quantities divisible by these fractional parts simplifies inventory management.
- For instance, purchasing 28 red chairs (since $\frac{2}{5} \times 140 = 56$) or 20 blue chairs ensures alignment with the calculated distribution.

Practical Considerations

- Uniformity: Ensuring chairs match in style but differ in color requires careful planning.
- Maintenance: Different colors may require different cleaning protocols.
- Accessibility: The color distribution might be designed to designate specific zones or functions within the hall.

Extensions and Variations of the Problem

While this scenario is straightforward, it opens avenues for exploring related questions:

- What if the number of yellow chairs was different?

Adjusting the given (Y) allows for recalculating (T) and the distribution, illustrating how fractional relationships adapt to changing parameters.

- What if the fractions of red and blue chairs changed?

This involves reworking the algebra with new fractions, demonstrating flexibility in planning.

- How does the distribution change with additional constraints?

For example, ensuring the number of chairs per color is divisible by a certain number for manufacturing purposes.

Conclusion: Synthesis of Mathematical Precision and Practical Application

This exploration exemplifies how fractional calculations and algebraic reasoning underpin real-world logistical challenges, such as furniture distribution in a school hall. By meticulously analyzing the problem, we confirmed that with 140 chairs in total, the specified distribution aligns perfectly with the given fractional data and explicit count of yellow chairs.

Such detailed analysis not only ensures accuracy but also enhances understanding of proportional reasoning, resource planning, and design considerations. Whether for educational environments, event management, or space planning, mastering these mathematical concepts provides a robust foundation for informed decision-making and effective resource utilization.

In summary, a school hall with 140 chairs arranged such that $\frac{2}{5}$ are red, $\frac{3}{7}$ are blue, and the remaining 24 are yellow offers a compelling case study in fractional distribution, resource planning, and spatial aesthetics. The detailed breakdown underscores the importance of mathematical literacy in everyday logistical and design challenges, making it an essential skill for educators, planners, and enthusiasts alike.

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