

Starting From Rest, A 10.0 Kg Suitcase Slides 3.00 M down A Frictionless Ramp Inclined At 30.0 From

Starting From Rest, A 10.0 Kg Suitcase Slides 3.00 M down A Frictionless Ramp Inclined At 30.0 From is a classic physics problem that explores the principles of motion, energy conservation, and forces on an inclined plane. This scenario involves analyzing the behavior of a suitcase sliding down an inclined, frictionless ramp, providing an excellent opportunity to understand key concepts such as gravitational potential energy, kinetic energy, acceleration, and the effects of inclination angles on motion. In this comprehensive guide, we will delve into the problem's details, outline the relevant physics principles, and walk through step-by-step calculations to determine the suitcase's velocity at the bottom of the ramp, as well as other related quantities.

Understanding the Scenario

Problem Description

The problem involves a suitcase with a mass of 10.0 kg placed at the top of a frictionless ramp inclined at 30.0 degrees relative to the horizontal. The suitcase is initially at rest and allowed to slide down the incline over a distance of 3.00 meters. The key questions typically posed in such problems include:

- What is the velocity of the suitcase at the bottom of the ramp?
- How much kinetic energy does the suitcase have at the bottom?
- How do the forces acting on the suitcase influence its motion?

Key Assumptions

To simplify the analysis, certain assumptions are made:

- The ramp is frictionless, meaning no energy is dissipated due to friction.
- The suitcase starts from rest.
- The incline angle remains constant at 30.0 degrees.
- Air resistance is negligible.
- The only significant forces are gravity and the normal force exerted by the ramp.

Fundamental Physics Principles Involved

Newton's Laws of Motion

Newton's second law states that the net force acting on an object equals its mass times its acceleration ($F = ma$). In the context of the inclined plane:

- Components of gravitational force influence the acceleration.
- The normal force balances the perpendicular component of gravity.
- The net force along the incline causes acceleration down the slope.

Energy Conservation

The principle of conservation of energy states that, in the absence of non-conservative forces like friction, the total mechanical energy remains constant. Therefore:

- The initial gravitational potential energy at the top converts into kinetic energy at the bottom.
- Mathematically:

$$(PE_{\text{initial}} + KE_{\text{initial}} = PE_{\text{final}} + KE_{\text{final}})$$

Since the suitcase starts from rest, initial kinetic energy is zero, and the initial potential energy depends on height.

Kinematic Equations

These equations relate velocity, acceleration, and displacement and are useful if calculating the velocity after sliding a certain distance.

Calculating the Height and Components of Forces

Determining the Height of the Incline

Given the length of the ramp and the incline angle, the vertical height (h) of the top point relative to the bottom is:

$$[h = L \sin(\theta)]$$

Where:

- ($L = 3.00 \text{ m}$) (length of the ramp)
- ($\theta = 30.0^\circ$)

Calculating:

$$h = 3.00 \text{ m} \times \sin(30.0^\circ) = 3.00 \text{ m} \times 0.5 = 1.50 \text{ m}$$

This height is critical for calculating the potential energy.

Calculating Gravitational Potential Energy at the Top

The initial potential energy:

$$PE_{\text{initial}} = m \times g \times h$$

Where:

- $m = 10.0 \text{ kg}$
- $g = 9.80 \text{ m/s}^2$

Calculating:

$$PE_{\text{initial}} = 10.0 \text{ kg} \times 9.80 \text{ m/s}^2 \times 1.50 \text{ m} = 147 \text{ J}$$

Since the ramp is frictionless, this potential energy converts into kinetic energy at the bottom.

Determining the Final Velocity at the Bottom

Using Conservation of Mechanical Energy

The total energy at the top:

$$E_{\text{total}} = PE_{\text{initial}}$$

At the bottom, the potential energy is zero (assuming the bottom is our reference point), and the kinetic energy is:

$$KE_{\text{final}} = \frac{1}{2} m v^2$$

Applying energy conservation:

$$PE_{\text{initial}} = KE_{\text{final}}$$

$$147 \text{ J} = \frac{1}{2} \times 10.0 \text{ kg} \times v^2$$

Solving for v :

$$v^2 = \frac{2 \times 147 \text{ J}}{10.0 \text{ kg}} = 29.4 \frac{\text{m}^2}{\text{s}^2}$$

$$v = \sqrt{29.4} \approx 5.42 \text{ m/s}$$

Therefore, the suitcase's velocity at the bottom of the ramp is approximately 5.42 m/s.

Alternative Approach: Using Kinematic Equations

If the initial velocity is zero and the acceleration a is constant, we can use:

$$v^2 = 2 a s$$

Where:

- $s = 3.00 \text{ m}$
- a is the acceleration along the incline.

The acceleration component along the incline:

$$a = g \sin(\theta) = 9.80 \frac{\text{m}}{\text{s}^2} \times 0.5 = 4.90 \frac{\text{m}}{\text{s}^2}$$

Calculating:

$$v^2 = 2 \times 4.90 \frac{\text{m}}{\text{s}^2} \times 3.00 \text{ m} = 29.4 \frac{\text{m}^2}{\text{s}^2}$$

$$v = \sqrt{29.4} \approx 5.42 \text{ m/s}$$

This confirms our earlier energy-based calculation.

Forces Acting on the Suitcase

Gravity and Normal Force

The primary forces are:

- Gravitational Force (Weight):

$$F_g = m \times g = 10.0 \text{ kg} \times 9.80 \frac{\text{m}}{\text{s}^2} = 98 \text{ N}$$

- Normal Force (perpendicular to the surface):

$$F_N = F_g \times \cos(\theta) = 98 \text{ N} \times \cos(30^\circ) \approx 98 \text{ N} \times 0.866 = 84.8 \text{ N}$$

- Component of gravity along the incline:

$$F_{\parallel} = F_g \sin(\theta) = 98\text{ N} \times 0.5 = 49\text{ N}$$

Net Force and Acceleration

Since the ramp is frictionless, the net force along the incline is:

$$F_{\text{net}} = F_{\parallel} = 49\text{ N}$$

And the acceleration:

$$a = \frac{F_{\text{net}}}{m} = \frac{49\text{ N}}{10.0\text{ kg}} = 4.90\text{ m/s}^2$$

This matches the earlier calculations.

Additional Considerations and Real-World Applications

Effect of Friction

In real-world scenarios, friction could significantly reduce the final velocity. The coefficient of kinetic friction (μ_k) between the suitcase and the ramp would introduce a resistive force:

$$F_{\text{friction}} = \mu_k F_N$$

This would decrease the net force and, consequently, the acceleration, leading to a lower final velocity. Engineers and designers consider frictional forces when designing ramps or slides.

Energy Losses and Safety Margins

Understanding the energy transformations in frictionless versus real systems helps in designing safer, more efficient transportation and loading systems. For example, ensuring that a suitcase or cargo doesn't slide uncontrollably requires considering these forces.

Applications in Engineering and Physics Education

Problems like this are fundamental in physics education, illustrating concepts such as:

- Conservation of energy

- Forces on inclined planes
- The relationship between force, mass, and acceleration
- Real-world implications for transportation and safety design

Summary of Key Results

- Height of the top of the ramp: 1.50 meters
- Initial potential energy: 147 Joules
- Final velocity at bottom: approximately 5.42 m/s
- Acceleration along the incline: 4.

Frequently Asked Questions

What is the initial velocity of the suitcase at the top of the ramp?

The initial velocity is zero since the suitcase starts from rest.

How much kinetic energy does the suitcase gain after sliding 3.00 meters down the frictionless ramp?

The kinetic energy gained is equal to the potential energy lost, which is mgh , where h is the vertical height lost.

What is the vertical height the suitcase descends during the slide?

The height h can be calculated as $h = d \sin(\theta)$, which is $3.00 \text{ m} \sin(30^\circ) = 1.50 \text{ m}$.

What is the final velocity of the suitcase at the bottom of the ramp?

Using energy conservation, $v = \sqrt{2gh} = \sqrt{2 \cdot 9.8 \text{ m/s}^2 \cdot 1.50 \text{ m}} \approx 5.43 \text{ m/s}$.

How does the incline angle affect the speed of the suitcase at the bottom?

A steeper incline (larger θ) results in a greater vertical height and thus a higher final speed, assuming no friction.

What role does friction play in the motion of the suitcase on the ramp?

Since the ramp is frictionless, friction does not do any work; the motion is governed solely by gravity and initial conditions.

If the ramp length was increased to 5.00 m, how would that affect the final velocity?

The final velocity would increase because the suitcase would descend a greater vertical height, gaining more kinetic energy.

Can the work-energy theorem be used to analyze this problem?

Yes, it relates the work done by gravity (potential energy loss) to the kinetic energy gained by the suitcase.

What is the importance of the mass of the suitcase in this problem?

Since mass appears in both potential and kinetic energy calculations, it cancels out, making the final speed independent of the suitcase's mass.

Additional Resources

Starting From Rest, A 10.0 kg Suitcase Slides 3.00 m Down a Frictionless Ramp Inclined at 30.0° From Horizontal

Introduction

In the realm of classical mechanics, the motion of objects on inclined planes offers a fundamental yet insightful exploration into the principles of energy conservation, forces, and kinematics. The scenario of a suitcase starting from rest and sliding down a frictionless incline is a classic problem that encapsulates these core concepts. This analysis delves into the detailed physics behind such a situation, considering all relevant variables, and provides a comprehensive understanding of the dynamics involved.

Setting the Scene: The Problem Overview

Imagine a suitcase with a mass of 10.0 kg, initially at rest, positioned at the top of an inclined plane. The plane is 3.00 meters long and inclined at an angle of 30.0° relative to the horizontal. The ramp is idealized as frictionless, meaning no energy is lost to heat or

deformation. The primary objectives include determining:

- The speed of the suitcase at the bottom of the ramp.
- The time it takes for the suitcase to reach the bottom.
- The acceleration of the suitcase during its descent.
- The force components acting on the suitcase throughout the motion.

This problem is a quintessential illustration of energy transfer and Newtonian mechanics, providing a platform to apply various principles systematically.

Fundamental Principles and Assumptions

Before diving into calculations, it is essential to clarify the assumptions and fundamental physics principles:

- Frictionless Surface: No frictional forces act on the suitcase, simplifying the energy considerations.
- Constant Acceleration: The acceleration of the suitcase is uniform due to the consistent component of gravity along the incline.
- Rigid and Fixed Ramp: The incline does not deform or move, providing a stable frame of reference.
- Negligible Air Resistance: Air drag is ignored, which is reasonable for small objects over short distances.
- Initial Rest Condition: The suitcase starts from rest; initial velocity $(v_0 = 0)$.

Kinematic and Dynamic Analysis

1. Force Components and Acceleration

Gravity acts vertically downward with a magnitude $(g \approx 9.81, \mathrm{m/s^2})$. The component of gravity parallel to the incline is:

$$F_{g,\parallel} = mg \sin \theta$$

Where:

- $(m = 10.0, \mathrm{kg})$,
- $(g = 9.81, \mathrm{m/s^2})$,
- $(\theta = 30.0^\circ)$.

Calculating this:

$$F_{g,\parallel} = 10.0 \times 9.81 \times \sin(30^\circ) = 10.0 \times 9.81 \times 0.5 = 49.05, \mathrm{N}$$

The normal force exerted by the ramp on the suitcase is:

$$F_N = mg \cos \theta = 10.0 \times 9.81 \times \cos(30^\circ) \approx 10.0 \times 9.81 \times 0.8660 \approx 85.0, \text{ N}$$

Since the surface is frictionless, the normal force is perpendicular to the surface and does not oppose motion along the incline.

The net force along the incline is simply $(F_{g,\text{parallel}})$, leading to an acceleration (a) :

$$a = \frac{F_{g,\text{parallel}}}{m} = g \sin \theta$$

Substituting the known values:

$$a = 9.81 \times 0.5 = 4.905, \text{ m/s}^2$$

Key Point: The acceleration of the suitcase is constant and directed down the incline.

1. Calculating the Final Speed at the Bottom

Given the initial velocity $(v_0 = 0)$, acceleration $(a = 4.905, \text{ m/s}^2)$, and displacement $(s = 3.00, \text{ m})$, the final velocity (v) can be found using kinematic equations:

$$v^2 = v_0^2 + 2 a s$$

$$v^2 = 0 + 2 \times 4.905 \times 3.00 = 2 \times 4.905 \times 3$$

$$v^2 = 29.43$$

$$v = \sqrt{29.43} \approx 5.43, \text{ m/s}$$

Result:

$$\boxed{\text{Speed at bottom} \approx \mathbf{5.43\, \mathrm{m/s}}}$$

This value represents the magnitude of the velocity of the suitcase as it reaches the bottom of the incline.

2. Energy Perspective: Conservation of Mechanical Energy

The problem can also be approached through energy conservation:

$$\text{Initial Potential Energy} = \text{Final Kinetic Energy}$$

Since the ramp is frictionless, mechanical energy remains constant:

$$m g h = \frac{1}{2} m v^2$$

Where (h) is the vertical height difference between the top and bottom of the ramp.

Calculating the Vertical Height (h) :

$$h = s \sin \theta = 3.00 \times \sin(30^\circ) = 3.00 \times 0.5 = 1.50\, \mathrm{m}$$

Applying energy conservation:

$$m g h = \frac{1}{2} m v^2$$

$$g h = \frac{1}{2} v^2$$

$$v = \sqrt{2 g h}$$

Plugging in the numbers:

$$v = \sqrt{2 \times 9.81 \times 1.50} = \sqrt{29.43} \approx 5.43\, \mathrm{m/s}$$

\]

Confirmation: The energy-based approach confirms the kinematic calculation, illustrating the consistency of physics principles.

3. Time to Reach the Bottom

Knowing the acceleration and displacement, the time (t) taken to reach the bottom can be derived from the kinematic equation:

$$s = v_0 t + \frac{1}{2} a t^2$$

Since $(v_0 = 0)$:

$$s = \frac{1}{2} a t^2$$

Solving for (t) :

$$t = \sqrt{\frac{2s}{a}} = \sqrt{\frac{2 \times 3.00}{4.905}}$$

$$t = \sqrt{\frac{6.00}{4.905}} \approx \sqrt{1.22} \approx 1.10, \text{ s}$$

Result:

$$\boxed{\text{Time to reach bottom} \approx \mathbf{1.10, \text{ s}}}$$

This brief duration underscores the rapidity of descent under such acceleration.

4. Forces Acting During Descent

Understanding the forces acting on the suitcase provides insights into the physical interactions:

- Gravity: Acts vertically downward with magnitude $(98.1, \text{ N})$.
- Normal Force: Acts perpendicular to the ramp surface with magnitude approximately $($

85.0\, \mathrm{N} \).

- Component of Gravity along the Ramp: $(49.05\, \mathrm{N})$ propelling the suitcase downward.

Since the surface is frictionless, the only unbalanced force component along the incline is $(49.05\, \mathrm{N})$, resulting in the constant acceleration.

5. Additional Considerations and Variations

While the idealized scenario simplifies analysis, real-world situations may introduce additional factors:

- Friction: Real surfaces often have friction, which would oppose motion, reducing acceleration and final speed.
- Air Resistance: For objects moving at higher speeds or over longer distances, drag could play a role.
- Ramp Geometry: Variations in incline angle or irregularities could influence motion.
- Initial Conditions: Starting from rest simplifies calculations; initial push or initial velocity would alter outcomes.
- Mass Independence: Interestingly, the mass of the suitcase cancels out in the energy and acceleration calculations, illustrating a fundamental principle: in the absence of friction, all objects accelerate equally under gravity regardless of mass.

6. Practical Implications and Real-World Applications

Understanding the physics of a suitcase sliding down an incline, albeit idealized, has tangible applications:

- Luggage Design: Ensuring smooth sliding mechanisms for ease of handling.
- Safety Considerations: Preventing unintended acceleration or runaway luggage on inclined surfaces.
- Engineering of Ramps and Slides: Designing safe and efficient transport systems.
- Educational Demonstrations: Visualizing fundamental physics principles interactively.

7. Summary of Key Results

Quantity	Value	Explanation
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Acceleration (a)	$4.905\, \text{m/s}^2$	Gravity component along the incline
Final speed (v)	$5.43\, \text{m/s}$	Speed at the

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