

What Is The Frequency Of A Photon That Has The Same Momentum As A Neutron Moving With A Speed Of M/s?

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Understanding the relationship between particles at the quantum level is a fundamental aspect of modern physics. Among these particles, neutrons and photons play pivotal roles due to their unique properties and behaviors. Neutrons are electrically neutral subatomic particles found within atomic nuclei, possessing mass and following classical and quantum mechanical principles. Photons, on the other hand, are massless quanta of electromagnetic radiation, traveling at the speed of light and exhibiting both wave and particle characteristics.

One intriguing question in physics involves comparing the momentum of different particles, especially when their properties intersect at the quantum level. Specifically, what is the frequency of a photon that has the same momentum as a neutron moving at a particular speed? This question not only explores fundamental concepts of momentum and energy but also delves into wave-particle duality, special relativity, and quantum mechanics.

In this comprehensive article, we will explore the physics underlying this question step-by-step. We will begin by reviewing the basic properties of neutrons and photons, then derive the relevant formulas linking momentum, energy, and frequency, and finally apply these formulas to compute the photon frequency for a neutron moving at a given velocity. Along the way, we will discuss practical implications, real-world applications, and the significance of these calculations in scientific research.

Understanding Neutrons and Photons: Basic Properties

Before delving into the calculations, it is essential to understand the fundamental properties of neutrons and photons.

Properties of Neutrons

- Mass: The rest mass of a neutron is approximately $(m_n = 1.675 \times 10^{-27})$ kg.
- Charge: Neutrons are electrically neutral.
- Velocity: Neutrons can move at various speeds, from thermal velocities (~ 2200 m/s) to near-relativistic speeds.
- Quantum Behavior: As massive particles, neutrons exhibit both particle-like and wave-like behaviors, described by quantum mechanics.

Properties of Photons

- Mass: Photons are massless particles.
- Charge: Photons carry no electric charge.
- Speed: Photons always travel at the speed of light, $(c \approx 3.00 \times 10^8) \text{ m/s}$.
- Energy and Momentum: Despite being massless, photons carry energy and momentum, related to their frequency and wavelength.

Understanding these properties allows us to relate momentum, energy, and frequency for each particle.

Fundamental Concepts: Momentum, Energy, and Frequency

To find the frequency of a photon with the same momentum as a moving neutron, we need to understand how momentum, energy, and frequency relate for both particles.

Momentum of a Neutron

- For a particle with mass (m) moving at velocity (v) , classical momentum is:

$$p = m v$$

- However, at high velocities (close to (c)), relativistic effects become significant, and momentum is given by:

$$p = \gamma m v$$

where

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

- For most practical purposes involving neutrons moving at relatively slow speeds (compared to (c)), the non-relativistic approximation $(p \approx m v)$ suffices.

Energy of a Neutron

- Rest energy:

$$E_0 = m c^2$$

- Total energy (relativistic):

$$E = \gamma m c^2$$

- Kinetic energy:

$$K = (\gamma - 1) m c^2$$

Photon Energy and Momentum

- For a photon, energy and momentum are directly related:

$$E_{\text{photon}} = h \nu$$
$$p_{\text{photon}} = \frac{E_{\text{photon}}}{c} = \frac{h \nu}{c}$$

where:

- h is Planck's constant (6.626×10^{-34} Js),
- ν is the frequency of the photon.

Deriving the Relationship: Matching the Momentum

Our goal is to find the frequency ν of a photon whose momentum equals that of a moving neutron.

Step 1: Express the neutron's momentum

Assuming the neutron's velocity (v) is known, its momentum is:

$$p_n = \gamma m v$$

If (v) is non-relativistic ($(v \ll c)$), then:

$$p_n \approx m v$$

For relativistic speeds, use:

$$p_n = \frac{m v}{\sqrt{1 - \frac{v^2}{c^2}}}$$

Step 2: Set neutron momentum equal to photon momentum

Since the photon's momentum is:

$$p_{\text{photon}} = \frac{h \nu}{c}$$

The condition for the photon to have the same momentum as the neutron is:

$$\frac{h \nu}{c} = p_n$$

Therefore,

$$\nu = \frac{c p_n}{h}$$

Step 3: Final formula for the photon frequency

Depending on whether the neutron's speed is non-relativistic or relativistic, we use the respective expression for (p_n) :

- Non-relativistic case:

$$\nu = \frac{c m v}{h}$$

- Relativistic case:

$$\nu = \frac{c}{h} m v \sqrt{1 - \frac{v^2}{c^2}}$$

This formula allows us to compute the photon frequency directly once the neutron's mass and velocity are known.

Practical Calculation Example

Suppose a neutron moves with a certain speed (v) . To make the calculation concrete, let's consider two scenarios:

Scenario A: Non-Relativistic Neutron

- Speed: $(v = 1000 \text{ m/s})$

Scenario B: Near-Relativistic Neutron

- Speed: $(v = 0.8 c = 0.8 \times 3.00 \times 10^8 \text{ m/s} = 2.4 \times 10^8 \text{ m/s})$

Calculations for Scenario A: $(v = 1000 \text{ m/s})$

Using the non-relativistic approximation:

$$p_n \approx m v = (1.675 \times 10^{-27} \text{ kg}) \times 1000 \text{ m/s} = 1.675 \times 10^{-24} \text{ kg m/s}$$

Photon frequency:

$$\nu = \frac{c p_n}{h} = \frac{3.00 \times 10^8 \text{ m/s} \times 1.675 \times 10^{-24} \text{ kg m/s}}{6.626 \times 10^{-34} \text{ Js}}$$

Calculating numerator:

$$\begin{aligned} & 3.00 \times 10^8 \times 1.675 \times 10^{-24} = 5.025 \times 10^{-16} \\ & \end{aligned}$$

Then,

$$\begin{aligned} & \nu = \frac{5.025 \times 10^{-16}}{6.626 \times 10^{-34}} \approx 7.58 \times 10^{17}, \\ & \text{Hz} \end{aligned}$$

Result: The photon must have a frequency of approximately 7.58×10^{17} Hz to have the same momentum as a neutron moving at 1000 m/s.

Calculations for Scenario B: $(v = 0.8 c)$

First, compute the Lorentz factor:

$$\begin{aligned} & \gamma = \frac{1}{\sqrt{1 - (0.8)^2}} = \frac{1}{\sqrt{1 - 0.64}} = \frac{1}{\sqrt{0.36}} = \\ & \frac{1}{0.6} \approx 1.6667 \end{aligned}$$

Then, the neutron's relativistic momentum:

$$\begin{aligned} & p_n = \gamma m v = 1.6667 \times 1.675 \times 10^{-27}, \text{ kg} \times 2.4 \times 10^8, \\ & \text{m/s} \end{aligned}$$

Calculating:

$$\begin{aligned} & 1.6667 \times 1.675 \times 10^{-27} = 2.791 \times 10^{-27} \\ & \end{aligned}$$

and

$$\begin{aligned} & 2.791 \times 10^{-27} \times 2.4 \times 10^8 = 6.698 \times 10^{-19}, \text{ kg m/s} \\ & \end{aligned}$$

Photon frequency

Frequently Asked Questions

How do you calculate the frequency of a photon that has the same momentum as a neutron moving at a given speed?

You first determine the neutron's momentum using $p = mv$. Since the photon has the same momentum, its frequency can be found using the relation $p = h/\lambda$ and $c = \lambda\nu$, leading to $\nu = p c / h$, where h is Planck's constant, c is the speed of light, and p is the momentum.

What is the significance of matching the momentum of a photon to that of a moving neutron?

Matching the momentum allows us to find the photon's frequency that corresponds to the same energy-momentum relationship, illustrating the particle-wave duality and how quantum properties relate across different particles.

If a neutron moves at a certain speed, how does its momentum compare to the momentum of a photon with the same frequency?

A neutron's momentum depends on its mass and velocity ($p = mv$), which is usually much larger than the momentum of a photon with the same frequency, since photons are massless and their momentum is directly proportional to frequency ($p = h/\lambda$).

Can a photon have the same momentum as a neutron moving at a specific speed? How is this possible given their mass differences?

Yes, a photon can have the same momentum as a neutron at a particular speed by adjusting its frequency accordingly. Despite the mass difference, momentum depends on different factors: for the neutron, mass and velocity; for the photon, frequency and wavelength. Their momenta can be equal even though their masses differ.

What is the formula to find the frequency of a photon that shares momentum with a neutron moving at velocity M/s?

The frequency ν of the photon is given by $\nu = (p c) / h$, where $p = m M$ (neutron's momentum), c is the speed of light, and h is Planck's constant. So, $\nu = (m M c) / h$.

Additional Resources

What Is The Frequency Of A Photon That Has The Same Momentum As A Neutron Moving With A Speed Of M/s?

In the realm of quantum mechanics and relativistic physics, the interplay between particles of vastly different masses—such as photons and neutrons—presents intriguing questions about their fundamental properties. One such question that often arises in advanced physics discussions is: What is the frequency of a photon that has the same momentum as a neutron moving with a specific speed? This inquiry not only touches upon the core principles of wave-particle duality but also exemplifies the profound connection between energy, momentum, and wavelength in relativistic contexts.

This article aims to explore this question comprehensively, covering the necessary theoretical background, deriving the relevant formulas, and discussing the physical implications. By the end, readers will understand how to determine the photon's frequency when its momentum matches that of a neutron traveling at a given velocity, and appreciate the broader significance of these calculations in modern physics.

Understanding the Fundamental Concepts

Before delving into the calculations, it is essential to clarify several foundational concepts that underpin the problem.

Wave-Particle Duality and Photons

- Photons are quantum particles of electromagnetic radiation, characterized by zero rest mass and always traveling at the speed of light (c).
- They exhibit wave-particle duality, meaning they possess both particle-like and wave-like properties, described by their energy, momentum, and wavelength.
- The de Broglie wavelength (λ) of a photon relates to its momentum (p) via the de Broglie relation:

$$p = \frac{h}{\lambda}$$

where h is Planck's constant.

Neutron Properties

- Neutrons are subatomic particles with rest mass ($m_n \approx 1.675 \times 10^{-27} \text{ kg}$).
- They are electrically neutral and can be considered non-relativistic or relativistic depending on their velocity.
- When moving at a velocity (v), their relativistic momentum is given by:

$$p_n = \gamma m_n v$$

where

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

γ
is the Lorentz factor.

Relativistic Momentum and Energy Relations

- For particles with non-zero rest mass, the total energy is:

$$E = \gamma m c^2$$

- The momentum relates to energy and mass as:

$$p = \gamma m v$$

- For photons, which are massless, the energy and momentum are related by:

$$E_{\text{ph}} = pc$$

Deriving the Required Photon Frequency

The core problem is to find the frequency f of a photon whose momentum p_{ph} equals that of a neutron traveling at a certain velocity v . The steps involve:

1. Calculating the neutron's momentum at velocity v .
2. Equating this to the photon's momentum.
3. Deriving the photon's frequency from its momentum.

Step 1: Neutron Momentum at a Given Velocity

The relativistic momentum of the neutron is:

$$p_n = \gamma m_n v$$

where:

- m_n is the neutron rest mass.
- v is the neutron's velocity (in m/s).
- γ is the Lorentz factor:

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

\]

Given that $(c \approx 3.00 \times 10^8, \text{m/s})$, if (v) is known, (p_n) can be calculated directly.

Step 2: Equating Neutron Momentum to Photon Momentum

Since the photon's momentum is:

$$\begin{aligned} & \backslash \\ p_{\text{ph}} &= \frac{h}{\lambda} \\ & \backslash \end{aligned}$$

and its energy is:

$$\begin{aligned} & \backslash \\ E_{\text{ph}} &= h f \\ & \backslash \end{aligned}$$

we set:

$$\begin{aligned} & \backslash \\ p_{\text{ph}} &= p_n \\ & \backslash \end{aligned}$$

which implies:

$$\begin{aligned} & \backslash \\ \frac{h}{\lambda} &= \gamma m_n v \\ & \backslash \end{aligned}$$

Step 3: Expressing the Photon's Frequency

The photon's energy relates to its frequency by:

$$\begin{aligned} & \backslash \\ E_{\text{ph}} &= h f \\ & \backslash \end{aligned}$$

and its momentum by:

$$\begin{aligned} & \backslash \\ p_{\text{ph}} &= \frac{E_{\text{ph}}}{c} = \frac{h f}{c} \end{aligned}$$

\]

Combining these relations and the earlier equality:

\[

$$\frac{hf}{c} = \gamma m_n v$$

\]

solving for f :

\[

$$f = \frac{c \gamma m_n v}{h}$$

\]

Thus, the frequency of the photon is:

\[

$$\boxed{f = \frac{c \gamma m_n v}{h} \times \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}}$$

\]

This formula encapsulates the direct dependence of the photon's frequency on the neutron's velocity and fundamental constants.

Numerical Example and Physical Interpretation

To illustrate, suppose a neutron moves at a known velocity v . For example, consider:

- $v = 10^7 \text{ m/s}$ (a significant fraction of c)
- $m_n = 1.675 \times 10^{-27} \text{ kg}$
- $c = 3.00 \times 10^8 \text{ m/s}$
- $h = 6.626 \times 10^{-34} \text{ Js}$

Calculating γ :

\[

$$\gamma = \frac{1}{\sqrt{1 - \frac{(10^7)^2}{(3 \times 10^8)^2}}} = \frac{1}{\sqrt{1 - \frac{10^{14}}{9 \times 10^{16}}}} = \frac{1}{\sqrt{1 - 1.111 \times 10^{-3}}} \approx 1.000555$$

\]

Then, the photon frequency:

\[

$$f \approx \frac{(3 \times 10^8) \times (1.675 \times 10^{-27}) \times 10^7}{6.626 \times 10^{-34}} \times 1.000555$$

\]

Calculating numerator:

$$\frac{(3 \times 10^8) \times (1.675 \times 10^{-27}) \times 10^7}{6.626 \times 10^{-34}} = 3 \times 10^8 \times 1.675 \times 10^{-20} = 5.025 \times 10^{-12}$$

Dividing by (h) :

$$f \approx \frac{5.025 \times 10^{-12}}{6.626 \times 10^{-34}} \times 1.000555 \approx 7.588 \times 10^{21} \text{ Hz}$$

This extremely high frequency corresponds to high-energy gamma-ray photons, consistent with the large momentum involved.

Physical Implications and Applications

Understanding the frequency of a photon sharing the same momentum as a moving neutron has several implications:

- Quantum Scattering: When neutrons interact with electromagnetic fields, their momentum transfer can be conceptualized via photon analogs, aiding in modeling scattering processes.
- Particle-Wave Duality: This calculation exemplifies how massive particles can be associated with wave properties, with their momentum dictating the wavelength and frequency of hypothetical photons.
- Neutron Interferometry: In precision measurements, understanding the wave properties of neutrons, including their equivalent photon frequencies, informs experimental design.
- High-Energy Physics: The high frequencies involved underscore the energies necessary to match macroscopic particle momenta with photon energies, relevant in particle accelerators and astrophysical phenomena.

Limitations and Assumptions

While the derivation is straightforward, it relies on several assumptions:

- The neutron's velocity is known precisely, and relativistic effects are properly accounted for via (γ) .
- The photon is considered ideal, massless, and propagating in a vacuum.

- The interaction between the neutron and photon is purely theoretical in this context; real particles do not convert their momentum into photons unless involved in electromagnetic interactions.

Conclusion

The frequency of a photon that possesses the same momentum as a neutron moving at velocity (v) can be succinctly expressed as:

$$f = \frac{c}{\lambda} = \frac{m_n v}{h} \times \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

This relation underscores the profound interconnectedness of mass, velocity, and wave properties in relativistic quantum mechanics. It bridges the classical and quantum worlds, illustrating how particles of vastly different masses can be related through their fundamental wave characteristics.

Understanding these principles deepens our grasp of particle physics and serves as a foundation for exploring

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