

A Duopoly Faces The Inverse Demand $P = 160 - 2q$ Both Firms In The Industry Have Constant Costs Of \$10 Per

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In the landscape of microeconomics, understanding how duopolies operate under different demand conditions and cost structures is fundamental. This article explores a specific scenario where two firms compete within a market characterized by an inverse demand function of $P = 160 - 2q$, and both firms face constant costs of \$10 per unit. Analyzing this setup provides insights into strategic behaviors, equilibrium outcomes, and the implications for market efficiency. Whether you're an economist, a student, or a business strategist, grasping these concepts enhances your understanding of competitive dynamics in differentiated or homogeneous markets.

Understanding the Market Structure and Demand Function

The Nature of a Duopoly

A duopoly is a market structure where only two firms dominate the industry. These firms are interdependent, meaning each firm's decision on pricing and quantity affects the other's outcomes. Unlike perfect competition, where numerous small firms compete, duopolies often lead to strategic interactions modeled through game theory, with outcomes like Cournot, Bertrand, or Stackelberg equilibria.

The Inverse Demand Function: $P = 160 - 2q$

The inverse demand function relates the market price (P) to the total quantity supplied (q). Here,

- $P = 160 - 2q$
- $q = q_1 + q_2$ (the sum of quantities produced by Firm 1 and Firm 2)

This linear inverse demand implies that as total output in the market increases, the price decreases at a rate of 2 per unit increase in total quantity. The intercept (160) signifies the maximum price when no units are supplied, while the slope (-2) indicates the sensitivity of price to quantity changes.

Cost Structure and Its Impact on Firm Strategies

Constant Costs of S10 Per Unit

Both firms face a constant marginal and average cost of S10 per unit. This cost structure simplifies analysis since the cost per unit remains unchanged regardless of output levels, contrasting with increasing or decreasing cost scenarios.

Implications of Constant Costs

- The firms will only produce profitably if the market price exceeds S10.
- The minimum acceptable price for profit-maximizing production is S10.
- The competitive and strategic behaviors hinge on how the equilibrium price compares to this cost.

Profit Maximization and Equilibrium Analysis

Setting Up the Profit Function

For each firm, profit (π) is calculated as:

$$\pi_i = (P - C) q_i$$

where:

- $P = 160 - 2(q_1 + q_2)$
- $C = 10$ (constant cost)
- q_i = quantity produced by firm i

Substituting P into the profit function:

$$\begin{aligned}\pi_i &= (160 - 2(q_1 + q_2) - 10) q_i \\ &= (150 - 2(q_1 + q_2)) q_i\end{aligned}$$

Deriving the Best Response Functions

Each firm chooses q_i to maximize its profit, taking the other firm's quantity as given. The first-order condition (FOC) for profit maximization:

$$\partial \pi_i / \partial q_i = 0$$

Calculating:

$$\partial \pi_i / \partial q_i = 150 - 2(q_1 + q_2) - 2q_i = 0$$

Rearranged:

$$\begin{aligned}150 - 2q_j - 2q_i - 2q_i &= 0 \\ \Rightarrow 150 - 2q_j - 4q_i &= 0\end{aligned}$$

Expressing q_i as a function of q_j :

$$\begin{aligned}4q_i &= 150 - 2q_j \\ \Rightarrow q_i &= (150 - 2q_j) / 4 \\ \Rightarrow q_i &= 37.5 - 0.5q_j\end{aligned}$$

Similarly, for Firm 2:

$$q_2 = 37.5 - 0.5q_1$$

These are the best response functions, indicating each firm's optimal output depends on the other's choice.

Finding the Cournot Equilibrium

Solving the System of Best Response Functions

Set $q_1 = q_2 = q$ at equilibrium:

$$q = 37.5 - 0.5q$$

Rearranged:

$$q + 0.5q = 37.5$$

$$\Rightarrow 1.5q = 37.5$$

$$\Rightarrow q = 37.5 / 1.5$$

$$\Rightarrow q = 25$$

Thus, the Cournot equilibrium quantities are:

$$- q_1 = q_2 = 25 \text{ units}$$

Total market quantity:

$$q_{\text{total}} = q_1 + q_2 = 50 \text{ units}$$

Market price:

$$P = 160 - 2(50) = 160 - 100 = \$60$$

Profit at Equilibrium

Profit per firm:

$$\pi_i = (P - C) q_i = (60 - 10) 25 = 50 \cdot 25 = \$1250$$

Each firm earns \$1250 profit, and the industry total profit is \$2500.

Market Outcomes and Efficiency Analysis

Market Price and Consumer Surplus

The equilibrium price of \$60 exceeds the constant marginal cost of \$10, indicating positive producer profits. Consumers benefit from the lower price compared to the maximum price (\$160), but the quantity produced is less than the perfectly competitive level.

Consumer surplus (CS):

$$CS = 0.5 (\text{Maximum price} - \text{Market price}) \text{ Quantity}$$

$$= 0.5 (160 - 60) 50$$

$$= 0.5 100 50 = \$2500$$

Social Welfare and Deadweight Loss

Compared to perfect competition, where firms would produce at $P = C = \$10$, the duopoly produces less, leading to deadweight loss. The market inefficiency arises from the strategic behaviors that limit output to sustain higher prices.

Strategic Considerations and Potential Variations

Impact of Cost Changes

If costs increase above \$10, firms might reduce output or exit the market. Conversely, lower costs could intensify competition, potentially eroding profits.

Alternative Competition Models

- Bertrand Model: If firms compete on prices rather than quantities, the equilibrium price may drop to marginal cost (\$10), eroding profits.
- Stackelberg Model: Leader-follower dynamics could lead to different equilibrium outputs and profits.

Market Power and Collusion

In some cases, firms might collude to set prices or output levels to maximize joint profits, potentially leading to higher prices and reduced consumer surplus.

Conclusion: Strategic Insights and Policy Implications

The scenario of a duopoly facing the inverse demand function $P = 160 - 2q$ with constant costs of \$10 per unit exemplifies classic oligopolistic behavior. The equilibrium analysis demonstrates that firms produce 25 units each, leading to a market price of \$60 and significant profits. However, the market outcome reveals inefficiencies compared to perfect competition, notably in reduced output and consumer surplus.

Understanding these dynamics assists policymakers in evaluating the need for regulations to prevent market power abuse or promote competition. For firms, recognizing the strategic interplay helps in making informed decisions about production levels, pricing strategies, and potential entry or exit.

In summary, the interaction between demand, costs, and strategic behavior in a duopoly significantly shapes market outcomes. Recognizing the factors that influence equilibrium quantities and prices enables better analysis of real-world markets, guiding effective economic decisions and

policies.

Key Takeaways:

- In a duopoly with inverse demand $P = 160 - 2q$ and constant costs of \$10, firms produce 25 units each at equilibrium.
- The market price settles at \$60, yielding profits of \$1250 per firm.
- The market outcome features positive profits but less output than perfect competition, leading to deadweight loss.
- Strategic interactions shape the equilibrium, with potential variations under different game-theoretic models.

This comprehensive analysis underscores the importance of demand functions, cost structures, and strategic decision-making in determining market performance and efficiency.

Frequently Asked Questions

What is the inverse demand function in the duopoly model $P = 160 - 2q$?

The inverse demand function is $P = 160 - 2q$, where P is the price and q is the total quantity supplied by both firms.

How do constant costs of \$10 per unit impact the firms' profit calculations?

Constant costs of \$10 per unit mean each firm's profit depends on the difference between the price and \$10, multiplied by their output quantity, influencing their production decisions.

What is the Cournot equilibrium in this duopoly setting?

The Cournot equilibrium occurs when both firms choose quantities where neither can improve their profit by unilaterally changing their output, given the other firm's choice, resulting in specific equilibrium quantities and prices derived from the inverse demand and cost functions.

How do the firms determine their optimal output levels in this duopoly?

Each firm maximizes its profit by setting its marginal revenue equal to constant marginal cost (\$10), considering the other firm's output, leading to a best-response function that determines the equilibrium quantities.

What is the total market quantity at equilibrium?

The total market quantity at equilibrium can be calculated by solving the firms' best-response

functions simultaneously, typically resulting in a specific numerical value based on the inverse demand and cost parameters.

How does the constant marginal cost of S10 influence the market price at equilibrium?

Since the market price depends on total quantity, the equilibrium price will be above the marginal cost S10, determined by the inverse demand when the equilibrium quantity is supplied.

What are the key assumptions of this duopoly model?

The key assumptions include constant marginal costs of S10, inverse demand $P = 160 - 2q$, firms choose quantities simultaneously, and firms aim to maximize profits without considering strategic entry or external shocks.

How does increasing the constant cost S10 affect the equilibrium outcomes?

Higher constant costs reduce firms' incentives to produce large quantities, potentially lowering equilibrium output levels and increasing market prices, depending on the demand elasticity.

Can this duopoly model be extended to include strategic behavior or capacity constraints?

Yes, the model can be extended to incorporate strategic behaviors like signaling or capacity constraints, which would alter firms' optimal decisions and could lead to different equilibrium outcomes.

What real-world industries can be modeled as a duopoly with constant costs and inverse demand similar to $P=160 - 2q$?

Industries such as airline routes, telecommunications providers, or regional energy suppliers often resemble this model, where firms face constant marginal costs and face downward-sloping demand curves.

Additional Resources

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In the realm of industrial organization and microeconomic theory, the study of duopolies—markets dominated by two firms—is fundamental for understanding strategic interactions, pricing behaviors, and market outcomes. The scenario where both firms face identical constant costs of S10 per unit and confront an inverse demand function of $P = 160 - 2q$ provides a rich framework for analyzing competitive and collusive behaviors, equilibrium strategies, and welfare implications. This article offers a comprehensive review of this model, exploring its theoretical foundations, strategic

implications, and the insights it offers into real-world markets.

Understanding the Model: Key Assumptions and Setup

Inverse Demand Function: $P = 160 - 2q$

The inverse demand function $P = 160 - 2q$ describes how the price (P) responds to the total quantity (q) supplied by both firms. Here, $q = q_1 + q_2$, where q_1 and q_2 are the quantities produced by Firm 1 and Firm 2, respectively. This linear demand indicates that as total industry output increases, the market price drops at a rate of 2 units per additional unit supplied.

Features:

- The intercept of 160 suggests the maximum price when no units are produced.
- The slope of -2 indicates the market's price sensitivity to total output.

Implications:

- Both firms face the same demand curve, making their strategic decisions symmetric.
- The linearity simplifies analysis and helps derive explicit equilibrium solutions.

Constant Costs of \$10 Per Firm

Each firm incurs a constant marginal and fixed cost of \$10 per unit produced. This assumption simplifies the profit calculation to:

$$\text{Profit} = (\text{Price} - \text{Cost}) \times \text{Quantity}$$

which becomes:

$$\text{Profit} = (P - 10) \times q_k, \text{ where } q_k \text{ is the quantity produced by firm } k.$$

Features:

- No increasing or decreasing marginal costs: costs are flat at \$10.
- This allows for straightforward profit maximization without concern for changing costs at different output levels.

Implications:

- The constant cost structure makes the analysis tractable and highlights the effects of strategic

output choices on profits.

- The competitive equilibrium and collusive outcomes are directly influenced by this cost level.

Strategic Behavior in the Duopoly

Cournot Competition: Quantitative Strategic Interaction

In a Cournot model, each firm chooses its quantity simultaneously, aiming to maximize its profit given the other firm's choice. The equilibrium is characterized by each firm's best response function.

Deriving the Best Response:

- Each firm's profit function:

$$\pi_k = (P - 10) \times q_k = (160 - 2(q_1 + q_2) - 10) \times q_k$$

- Simplifies to:

$$\pi_k = (150 - 2q_1 - 2q_2) \times q_k$$

- Best response for Firm k:

To maximize π_k with respect to q_k :

$$d\pi_k/dq_k = 150 - 4q_k - 2q_{-k} = 0$$

Solving for q_k :

$$q_k = (150 - 2q_{-k}) / 4$$

Symmetric Equilibrium:

Assuming $q_1 = q_2 = q$, the equilibrium quantity:

$$q = (150 - 2q) / 4$$

$$4q = 150 - 2q$$

$$6q = 150$$

$$q = 25$$

Market Price at Cournot Equilibrium:

$$P = 160 - 2(25 + 25) = 160 - 100 = 60$$

Profits:

Profit per firm:

$$\pi = (60 - 10) \times 25 = 50 \times 25 = \$1250$$

Advantages:

- Clear, explicit equilibrium results.
- Demonstrates how strategic quantity choices influence market outcomes.

Disadvantages:

- Assumes simultaneous moves; in reality, firms may observe each other's actions.
- Ignores potential for collusion or cooperation.

Stackelberg Competition: Leader-Follower Dynamics

In a Stackelberg model, one firm acts as a leader, choosing quantity first, and the other as a follower, responding optimally.

Analysis:

- The leader anticipates the follower's best response:

$$q_{\text{follower}} = (150 - 2q_{\text{leader}}) / 4$$

- The leader maximizes its profit:

$$\pi_1 = (160 - 2(q_1 + q_2) - 10) \times q_1$$

Substituting q_2 :

$$\pi_1 = (150 - 2q_1 - 2[(150 - 2q_1)/4]) \times q_1$$

- Simplify and differentiate to find the optimal leader quantity.

Results:

- The leader produces more than in Cournot equilibrium, capturing a larger market share.
- The follower produces less, constrained by the leader's move.

Implications:

- The Stackelberg equilibrium typically results in higher profits for the leader.
- It demonstrates the strategic advantage of moving first.

Implications of the Model for Market Strategies

Pricing and Output Decisions

The analysis shows how firms' choices of quantities under duopoly influence the market price and profits. Firms balancing their output to avoid oversupply, which depresses prices, can benefit from understanding these strategic equilibria.

Key insights:

- Both firms produce less than in perfect competition but more than in monopoly, balancing profits and market share.
- The equilibrium quantities are sensitive to cost levels and demand elasticity.

Collusion and Market Power

While the model assumes non-cooperative behavior, the structure suggests that firms could benefit from collusion, effectively acting as a monopoly.

Pros of Collusion:

- Higher prices and profits for firms.
- Market stability.

Cons:

- Legal and regulatory risks.
- Risk of detection and punishment.

Features:

- The constant costs and demand structure make collusion more attractive theoretically.
- However, the temptation to cheat often undermines collusive agreements.

Welfare and Market Efficiency

Consumer Surplus and Deadweight Loss

Compared to a perfectly competitive market, the duopoly produces less output, leading to higher prices and reduced consumer surplus.

Calculations:

- Consumer surplus at equilibrium:

$$CS = 0.5 \times (\text{Maximum Price} - \text{Equilibrium Price}) \times \text{Equilibrium Quantity}$$

Maximum price is 160; equilibrium price is 60; quantity is 50 (25+25).

$$CS = 0.5 \times (160 - 60) \times 50 = 0.5 \times 100 \times 50 = \$2500$$

Deadweight Loss:

- The reduction in total surplus compared to perfect competition indicates inefficiency.

Implications:

- Consumers are worse off under duopoly than in perfect competition.
- Market inefficiency is inherent in strategic duopoly models.

Real-World Applications and Limitations

Applications:

- Oligopolistic industries such as airlines, telecommunications, and oil markets often resemble this model.
- Understanding strategic interactions helps regulators design policies to promote competition.

Limitations:

- Real markets often feature more than two firms, differentiated products, and dynamic strategies.
- Cost structures may not be constant; economies or diseconomies of scale influence outcomes.
- The assumption of symmetric firms simplifies analysis but may not reflect reality.

Conclusion: Insights and Policy Implications

The scenario of a duopoly facing the inverse demand $P=160 - 2q$ with constant costs of \$10 illustrates fundamental principles of industrial organization. The explicit derivation of Cournot and

Stackelberg equilibria demonstrates how strategic quantity choices shape market prices, profits, and welfare outcomes. While the model's simplicity offers clarity, it also underscores the complexities of real-world markets, where strategic interaction, cost structures, and regulatory environments interplay.

Key takeaways:

- Duopolists tend to produce more than a monopolist but less than perfectly competitive firms.
- Strategic behavior can be exploited for competitive advantage, as seen in Stackelberg leadership.
- Welfare analysis underscores the trade-offs between firm profits and consumer surplus, highlighting the importance of market regulation.

Final thoughts:

Understanding such models equips policymakers and industry players with insights into the effects of competition and cooperation. Recognizing the potential for collusion, the impact of strategic moves, and the welfare implications can guide more informed decisions aimed at fostering competitive, efficient, and consumer-friendly markets.

Pros and Cons Summary:

Pros:

- Provides clear, explicit solutions for equilibrium quantities and prices.
- Demonstrates strategic interactions in a simplified framework.
- Highlights the effects of cost structures on market outcomes.
- Useful for educational purposes and policy analysis.

Cons:

- Assumes symmetry and simplicity that may not hold in real markets.
- Ignores product differentiation, entry barriers, and dynamic strategies.
- Constant costs may not reflect economies of scale.
- Does not account for externalities or regulatory constraints.

Overall, this model serves as a foundational tool for understanding duopoly behavior, offering valuable insights despite its limitations. It emphasizes that strategic decision-making profoundly influences market efficiency, pricing, and

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