

2. Consider This Dilation. Pre-image 9 Cm Image 3 Cm B(a) Find The Scale Factor. Show Your Work. (5 Points) (2-a.)

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Understanding Dilation in Geometry

Geometry often involves transformations that change the size or position of figures. One such transformation is dilation, which enlarges or reduces a figure proportionally from a fixed point called the center of dilation. When analyzing dilations, a key concept is the scale factor, which quantifies how much the image has been scaled relative to the pre-image.

In this guide, we'll dissect the problem involving a dilation where the pre-image measures 9 centimeters, and the resulting image measures 3 centimeters. Our primary goal is to find the scale factor of this dilation, ensuring clarity in how to approach and solve such problems systematically.

What Is a Scale Factor in Dilation?

Definition of Scale Factor

The scale factor of a dilation is a number that describes how much the original figure (pre-image) is enlarged or reduced to produce the image. It is expressed as a ratio or a decimal, representing the proportional change in size.

Interpreting Scale Factors

- If the scale factor is greater than 1, the figure is enlarged.
- If the scale factor is between 0 and 1, the figure is reduced.
- A scale factor of exactly 1 means the figure remains unchanged.

Given Data and Problem Breakdown

Let's analyze the problem details:

- Pre-image length: 9 cm
- Image length: 3 cm
- Objective: Find the scale factor of the dilation

The problem mentions "B(a)", which might refer to a specific point or label within a figure, but for the purpose of calculating the scale factor, the critical data are the lengths of the pre-image and image.

Step-by-Step Solution Approach

To find the scale factor, we need to compare the size of the image to the pre-image. The general formula for scale factor (k) in dilation is:

$$k = \frac{\text{Length of Image}}{\text{Length of Pre-image}}$$

Step 1: Identify known lengths

- Pre-image length: 9 cm
- Image length: 3 cm

Step 2: Set up the ratio

$$k = \frac{3 \text{ cm}}{9 \text{ cm}}$$

Step 3: Simplify the ratio

$$k = \frac{1}{3}$$

Step 4: Interpret the result

Since $k = \frac{1}{3}$, the image is a scaled-down version of the pre-image, reduced to one-third of its original size.

Final Answer and Explanation

The scale factor of the dilation is $\frac{1}{3}$.

This means:

- The figure has been reduced to 33.3% (or one-third) of its original size.
- The reduction is proportional, maintaining the shape's similarity but changing the size.

Additional Considerations in Dilation Problems

While this problem is straightforward, understanding some broader concepts can help tackle similar questions more effectively:

1. Center of Dilation

- The point from which the figure is dilated.
- Not specified here, but essential for understanding the transformation.

2. Types of Dilation

- Enlargement: Scale factor > 1
- Reduction: $0 < \text{Scale factor} < 1$
- No change: Scale factor $= 1$

3. Effects of Dilation on Coordinates

When figures are plotted on coordinate planes, dilation affects the coordinates according to the scale factor and the center of dilation.

4. Real-World Applications

- Architectural scaling
- Map reductions/enlargements
- Engineering designs

Practical Tips for Solving Dilation Scale Factor Problems

- Always identify the given lengths clearly.
- Use the formula $k = \frac{\text{Image length}}{\text{Pre-image length}}$.
- Check whether the scale factor indicates enlargement (>1) or reduction (<1).
- Ensure units are consistent to avoid calculation errors.
- Remember that in similar figures, all corresponding lengths are scaled by the same factor.

Common Mistakes to Avoid

1. Using the wrong numerator and denominator in the ratio; always divide the image length by the pre-image length.
2. Assuming the scale factor is the difference in lengths rather than their ratio.
3. Ignoring units; ensure measurements are in the same units before calculating.
4. Confusing scale factor with scale size; the factor is a ratio, not a measurement.

Summary

- The problem involves a dilation with a pre-image length of 9 cm and an image length of 3 cm.
- The scale factor is calculated as $\left(\frac{3}{9} = \frac{1}{3} \right)$.
- The figure has been reduced to one-third of its original size.
- Understanding the concept of scale factor is vital for solving similar geometry problems involving dilations.
- Always double-check calculations and interpret the scale factor in the context of the problem.

Conclusion

Understanding how to find the scale factor in dilation problems is fundamental in geometry, especially in similarity and transformations. By carefully analyzing the given lengths and applying the ratio, you can efficiently determine the scale factor and understand how figures relate to each other in size. Remember, the key steps involve identifying the known lengths, setting up the ratio correctly, simplifying, and interpreting the result appropriately. Mastery of these steps enhances problem-solving skills and deepens your comprehension of geometric transformations.

Frequently Asked Questions

What is the scale factor in a dilation when the pre-image length is 9 cm and the image length is 3 cm?

The scale factor is found by dividing the image length by the pre-image length: $3 \text{ cm} \div 9 \text{ cm} = 1/3$ or approximately 0.33.

How do you calculate the scale factor for a dilation given the pre-image and image sizes?

Divide the length of the image by the length of the pre-image. In this case, $3 \text{ cm} \div 9 \text{ cm} = 1/3$.

If a pre-image measures 9 cm and its dilated image measures 3 cm, what is the scale factor? Show your work.

Scale factor = image size $\div$ pre-image size = $3 \text{ cm} \div 9 \text{ cm} = 1/3$.

What does a scale factor of $1/3$ indicate about the dilation process?

It indicates that the image is one-third the size of the pre-image, meaning the figure has been reduced to a third of its original size.

Is the scale factor in this problem greater than, less than, or equal to 1? What does that imply?

The scale factor is less than 1 ($1/3$), which implies the image is a reduction of the original figure.

Can the scale factor be expressed as a decimal? If so, what is it for this problem?

Yes, the scale factor as a decimal is approximately 0.33.

Why is it important to show your work when calculating the scale factor in a dilation?

Showing work ensures accuracy, helps understand the process, and allows others to verify your calculations.

What is the significance of the scale factor in similar figures?

The scale factor determines how much the figure has been enlarged or reduced, maintaining proportionality between similar figures.

If the scale factor is $1/3$, what is the ratio of the image to the pre-image?

The ratio of the image to the pre-image is 1:3.

How would you find the original pre-image length if the image length and scale factor are known?

Divide the image length by the scale factor: pre-image length = image length

$\div$ scale factor. For example, if the image is 3 cm and scale factor is $1/3$, then pre-image = $3 \text{ cm} \div (1/3) = 9 \text{ cm}$.

Additional Resources

Consider This Dilation: An In-Depth Exploration of Scale Factors in Geometric Transformations

In the realm of geometry, transformations serve as fundamental tools that allow mathematicians and students alike to understand the relationships and properties of shapes. Among these transformations, dilation stands out for its ability to produce similar figures through resizing while maintaining shape integrity. The problem at hand – "Consider This Dilation. Pre-image 9 cm, Image 3 cm. Find the Scale Factor. Show Your Work." – encapsulates a core concept that is pivotal in understanding how figures are proportionally related through dilation. This article delves into the intricacies of dilation, unpacks the steps involved in determining scale factors, and explores the broader implications of this transformation in mathematical reasoning and real-world applications.

Understanding Dilation in Geometry

Dilation, also known as resizing or enlargement/reduction, is a transformation that produces an image that is the same shape as the original (pre-image) but scaled by a certain factor. Unlike rigid transformations such as translations, rotations, or reflections, dilation alters the size of a figure but preserves angles and the proportional relationships between sides.

Key Concepts of Dilation

- Center of Dilation: The fixed point about which the figure is enlarged or reduced.
- Scale Factor (k): The ratio that defines how much the figure is enlarged or reduced. If $k > 1$, the figure is enlarged; if $0 < k < 1$, the figure is reduced.
- Pre-image and Image: The original figure before dilation is called the pre-image; after dilation, the resulting figure is called the image.

Mathematical Representation

Dilation can be expressed mathematically as:

$$[\text{Image}] = k \times [\text{Pre-image}]$$

where all linear measurements of the image are scaled by the factor k relative to the pre-image.

Analyzing the Problem: Finding the Scale Factor

Given the problem:

- Pre-image length = 9 cm
- Image length = 3 cm

The core question: What is the scale factor of the dilation?

Step-by-Step Solution

1. Identify the Known Quantities:

- Pre-image length (original figure): 9 cm
- Image length (after dilation): 3 cm

2. Set Up the Ratio:

Since dilation scales all dimensions proportionally,

$$\left[k = \frac{\text{Image length}}{\text{Pre-image length}} \right]$$

3. Calculate the Scale Factor:

$$\left[\begin{aligned} k &= \frac{3 \text{ cm}}{9 \text{ cm}} = \frac{1}{3} \end{aligned} \right]$$

4. Interpretation:

- The scale factor is $\left(\frac{1}{3}\right)$, indicating the image is a reduction of the original by a factor of one-third.
- This confirms that the dilation is a reduction, not an enlargement.

Conclusion of the Calculation

The scale factor for this dilation is $\left(\boxed{\frac{1}{3}}\right)$. This indicates that every linear measurement in the image is one-third of the corresponding measurement in the pre-image.

Deeper Insights: Implications and Related Concepts

Understanding scale factors in dilation extends beyond simple calculations; it unlocks a broader comprehension of geometric similarity, proportional reasoning, and their applications.

Properties of Dilation

- Similarity: Dilation creates similar figures, which means their

corresponding angles are equal, and their sides are proportional by the scale factor.

- Area and Volume: While linear dimensions scale linearly, areas and volumes scale by the square and cube of the scale factor, respectively.

For example:

- Area scale factor = (k^2)

- Volume scale factor = (k^3)

- Preservation of Angles: Dilation preserves angles, maintaining the shape's internal characteristics.

Practical Applications of Dilation and Scale Factors

- Architecture and Engineering: Architects use scale models to represent real structures, employing scale factors to accurately depict proportions.

- Cartography: Maps are scaled-down versions of geographic areas, with scale factors ensuring accurate representation.

- Biology: Understanding how organisms grow involves concepts akin to dilation, where size changes occur proportionally.

- Art and Design: Artists utilize scale factors to create accurate enlargements or reductions of their work.

Common Misconceptions and Pitfalls in Calculating Scale Factors

While the concept appears straightforward, students often encounter misunderstandings:

- Confusing Pre-image and Image: Remember that the pre-image is the original figure; the image is the result after dilation.

- Incorrect Ratio Setup: Always ensure the ratio compares corresponding linear measurements.

- Ignoring Direction of Dilation: Whether the figure enlarges or reduces depends on the scale factor (>1 or <1).

Extending the Concept: From Lines to Complex Figures

The principles used in this simple problem extend to more complex figures:

- Composite Dilation: Combining multiple dilation steps with different scale factors.

- Coordinate Geometry: Applying dilation formulas to points in the coordinate plane.

For example, dilating a point $((x, y))$ about the origin involves:

$$[(x', y') = (k \times x, k \times y)]$$

This extends the concept of scale factors to coordinate transformations.

Final Thoughts: The Significance of This Dilation Problem

While at first glance, a problem asking for a scale factor might seem elementary, its implications reach into foundational principles of geometry. Recognizing that the scale factor is a ratio of corresponding measurements emphasizes proportional reasoning, a skill vital across mathematics and sciences.

This problem underscores the importance of precise calculations and conceptual understanding in geometric transformations. The deduction that the scale factor is $(\frac{1}{3})$ not only solves the immediate question but also reinforces the core idea that dilation preserves shape while scaling size proportionally.

In educational contexts, mastering such problems prepares students to approach more complex geometric concepts, from similarity and congruence to advanced transformations in coordinate geometry.

In Summary:

- Dilation involves resizing figures proportionally about a center point.
- The scale factor is calculated by dividing the image measurement by the pre-image measurement.
- For the given problem, the scale factor is $(\frac{1}{3})$, indicating a reduction.
- Understanding dilation and scale factors is crucial for grasping similarity, proportional reasoning, and their applications across various fields.
- Always approach these problems with clarity about what each measurement represents and ensure ratios are set up correctly.

Through diligent analysis and conceptual clarity, problems like "Consider This Dilation" become gateways to deeper understanding in geometry, illustrating the elegance and interconnectedness of mathematical principles.

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