

Consider The Following Absolute Value Inequality. $7x+8y+63\geq 8$ Rewrite The Given Inequality As Two Linear Inequalities.

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When working with absolute value inequalities, understanding how to rewrite them as two separate linear inequalities is essential for solving and analyzing the problem effectively. Absolute value expressions often represent distances or magnitudes, and their inequalities can be interpreted as conditions that restrict the values of variables within certain bounds. In this article, we will explore the process of transforming an absolute value inequality into two linear inequalities, using the given expression as a practical example.

Understanding Absolute Value Inequalities

Before delving into the specific inequality, it is crucial to grasp the fundamental concept of absolute value. The absolute value of a number or expression, denoted by $|x|$, measures its distance from zero on the number line, regardless of direction.

Key properties:

- $|x| \geq 0$ for all real x
- $|x| = x$ if $x \geq 0$
- $|x| = -x$ if $x < 0$

An absolute value inequality typically takes forms such as:

- $|\text{expression}| < a$
- $|\text{expression}| \leq a$
- $|\text{expression}| > a$
- $|\text{expression}| \geq a$

where a is a non-negative real number.

Rewriting Absolute Value Inequalities:

The general approach involves understanding that:

- $|\text{expression}| < a$ is equivalent to: $-a < \text{expression} < a$
- $|\text{expression}| \leq a$ is equivalent to: $-a \leq \text{expression} \leq a$
- $|\text{expression}| > a$ is equivalent to: $\text{expression} > a$ or $\text{expression} < -a$
- $|\text{expression}| \geq a$ is equivalent to: $\text{expression} \geq a$ or $\text{expression} \leq -a$

This fundamental principle allows us to convert absolute value inequalities into two separate linear inequalities, which are often easier to solve.

Analyzing the Given Inequality

Let's examine the specific inequality provided:

$$7x + 8y + 638$$

At first glance, this seems incomplete or possibly a typo. However, considering the context and typical algebraic structures, it appears to be an expression involving variables x and y with coefficients, possibly intended as:

$$|7x + 8y| + 638 < \text{some constant, or similar.}$$

Since the original prompt mentions "Rewrite the Given Inequality as Two Linear Inequalities," we can assume the intended inequality resembles an absolute value inequality of the form:

$$|7x + 8y| < c$$

for some constant c .

For the purpose of this article, let's consider the general case:

$$|7x + 8y| < 638$$

This example allows us to demonstrate the process of rewriting an absolute value inequality as two linear inequalities.

Rewriting Absolute Value Inequalities as Two Linear Inequalities

Given the inequality:

$$|7x + 8y| < 638$$

we can interpret this as:

- The expression $7x + 8y$ lies within 638 units of zero on the number line.

Applying the property:

$$|\text{expression}| < a \Leftrightarrow -a < \text{expression} < a$$

we obtain:

$$-638 < 7x + 8y < 638$$

This is a compound inequality, representing all points (x, y) where $7x + 8y$ is between -638 and 638.

Similarly, for inequalities involving " $\geq$ " or " $>$ ", the process involves rewriting as two separate inequalities:

$$|7x + 8y| \geq 638 \Leftrightarrow 7x + 8y \leq -638 \text{ or } 7x + 8y \geq 638$$

Step-by-Step Process to Rewrite the Inequality

1. Identify the absolute value expression:

Recognize the expression inside the absolute value, in this case, $7x + 8y$.

2. Determine the boundary constant:

The constant 638 in the inequality.

3. Apply the absolute value property:

For $|7x + 8y| < 638$, rewrite as:

$$-638 < 7x + 8y < 638$$

4. Express as two linear inequalities:

The inequalities are:

$$- 7x + 8y < 638$$

$$- 7x + 8y > -638$$

5. Combine or analyze the inequalities:

These two inequalities define the region of solutions for the original absolute value inequality.

Graphical Interpretation of the Inequalities

Visualizing these inequalities enhances understanding of the solution set.

The Boundary Lines

- The equations $7x + 8y = 638$ and $7x + 8y = -638$ are straight lines in the xy -plane.
- These lines are called the boundary lines, dividing the plane into regions.

The Solution Region

- The inequalities $7x + 8y < 638$ and $7x + 8y > -638$ describe the region between these two lines.
- Since the inequalities are strict ($<$ and $>$), the boundary lines are not included in the solution set (these are open regions).

Plotting the Lines

- To graph these lines, find intercepts:

For $7x + 8y = 638$:

- Set $x = 0$: $8y = 638 \Rightarrow y = 79.75$
- Set $y = 0$: $7x = 638 \Rightarrow x \approx 91.14$

For $7x + 8y = -638$:

- Set $x = 0$: $8y = -638 \Rightarrow y = -79.75$
- Set $y = 0$: $7x = -638 \Rightarrow x \approx -91.14$

Plot these points and draw the boundary lines.

Applications and Solving Strategies

Rewriting absolute value inequalities as two linear inequalities is a fundamental skill in algebra, with applications across various fields such as engineering, physics, and economics. Understanding the solution regions helps in:

- Determining feasible solutions in optimization problems
- Analyzing safety zones in engineering designs
- Evaluating inequalities in data analysis

Steps to solve such inequalities:

1. Rewrite the absolute value inequality as two linear inequalities.
2. Graph the boundary lines to visualize the solution region.
3. Determine which side of each boundary line satisfies the inequality.
4. Identify the intersection of these regions to find the solution set.
5. Check particular points to verify if they satisfy the original inequality.

Dealing with Other Variations of Absolute Value

Inequalities

Different forms of absolute value inequalities require slightly different approaches:

Inequality Type	Rewritten as	Solution Region
$ \text{expression} < a$	$-a < \text{expression} < a$	Inside the boundary
$ \text{expression} \leq a$	$-a \leq \text{expression} \leq a$	Inside or on the boundary
$ \text{expression} > a$	$\text{expression} > a$ or $\text{expression} < -a$	Outside the boundary
$ \text{expression} \geq a$	$\text{expression} \geq a$ or $\text{expression} \leq -a$	Outside or on the boundary

Note: When the inequality is non-strict ($\leq$ or $\geq$), the boundary lines are included in the solution set.

Example Problem with Complete Data

Suppose you are given the inequality:

$$|7x + 8y| + 638 \leq 1000$$

Step 1: Isolate the absolute value:

$$|7x + 8y| \leq 1000 - 638$$

$$|7x + 8y| \leq 362$$

Step 2: Rewrite as two inequalities:

$$-7x + 8y \leq 362$$

$$-7x + 8y \geq -362$$

Step 3: Plot and interpret the solution region:

$$\text{- Boundary lines: } 7x + 8y = 362 \text{ and } 7x + 8y = -362$$

- The solution region contains all points between these two lines.

Conclusion

Transforming absolute value inequalities into two linear inequalities simplifies the process of solving and analyzing the solution set. By understanding this fundamental principle, students and mathematicians can interpret complex inequalities geometrically and algebraically, leading to more efficient problem-solving strategies.

In the context of the example provided, assuming the inequality was of the form $|7x + 8y| < 638$, the rewrite process involved expressing it as $-638 < 7x + 8y < 638$. This method can be universally applied to a wide range of absolute value inequalities, forming a key part of algebraic problem-solving and mathematical reasoning.

Remember:

- Always identify the absolute value expression.
- Determine the boundary constant.
- Apply the property to rewrite as two inequalities.
- Use graphing to interpret the solution set visually.
- Check your solutions to ensure consistency with the original inequality.

By mastering these steps, you'll enhance your understanding of inequalities and their applications across mathematics and related disciplines.

Frequently Asked Questions

How do you rewrite the absolute value inequality $|7x + 8y + 638|$ as two separate linear inequalities?

You split the original inequality into two parts: one where $7x + 8y + 638$ is greater than or equal to zero, and another where it is less than or equal to zero. Specifically, rewrite as $7x + 8y + 638 \geq 0$ and $7x + 8y + 638 \leq 0$.

What is the significance of rewriting an absolute value inequality into two linear inequalities?

Rewriting helps to analyze and graph the solution set more easily by breaking down the absolute value condition into two linear cases, representing the regions where the expression inside the absolute value is positive or negative.

Given the inequality $|7x + 8y + 638|$, how do you determine the corresponding linear inequalities?

Identify the two cases: when $7x + 8y + 638 \geq 0$, the inequality remains $7x + 8y + 638 \leq$ some value; when $7x + 8y + 638 \leq 0$, it becomes $7x + 8y + 638 \geq$ negative of that value. In the absence of a specific bound, you simply set up the inequalities as ≥ 0 and ≤ 0 to analyze the regions.

Can you provide an example of rewriting $|7x + 8y + 638| \leq c$ as two inequalities?

Yes. For instance, $|7x + 8y + 638| \leq c$ can be rewritten as $-c \leq 7x + 8y + 638 \leq c$, which is two inequalities: $7x + 8y + 638 \leq c$ and $7x + 8y + 638 \geq -c$.

What steps are involved in converting the absolute value inequality $7x + 8y + 638 \leq 0$ into linear inequalities?

First, recognize that $|7x + 8y + 638| \leq 0$ implies $7x + 8y + 638 = 0$, since absolute value is never negative. Therefore, it reduces to the single linear equation $7x + 8y + 638 = 0$. For inequalities involving absolute value greater than or equal to a positive number, split into two inequalities accordingly.

Additional Resources

Consider The Following Absolute Value Inequality. $7x + 8y + 638$

Introduction

Mathematics, particularly algebra, is fundamental in developing critical thinking and problem-solving skills. Among algebraic concepts, inequalities involving absolute values hold special significance because they describe ranges of solutions rather than single points. This article thoroughly investigates the process of transforming a complex absolute value inequality into two linear inequalities, using the example:

Consider the following absolute value inequality: $7x + 8y + 638$.

Though the expression appears incomplete or possibly mistyped, the core concept remains the same: understanding how to interpret and manipulate absolute value inequalities. We will explore the principles behind such transformations, the step-by-step method to rewrite absolute value inequalities as linear inequalities, and the importance of these techniques in both academic and practical contexts.

Understanding Absolute Value Inequalities

What Is an Absolute Value?

The absolute value of a real number, denoted $|A|$, measures its distance from zero on the number line. For any real number A :

- $|A| \geq 0$
- $|A| = A$ if $A \geq 0$
- $|A| = -A$ if $A < 0$

This concept extends naturally to algebraic expressions, enabling us to describe a set of solutions where the "distance" between an expression and zero satisfies certain bounds.

General Form of Absolute Value Inequalities

An absolute value inequality typically takes the form:

$|Expression| < c$
 $|Expression| \leq c$
 $|Expression| > c$
 $|Expression| \geq c$

where c is a non-negative real number.

The key idea is that these inequalities can be rewritten as compound inequalities that define ranges of values for the variables involved. For example:

$|A| < c$ is equivalent to $-c < A < c$
 $|A| \leq c$ is equivalent to $-c \leq A \leq c$
 $|A| > c$ is equivalent to $A < -c$ or $A > c$
 $|A| \geq c$ is equivalent to $A \leq -c$ or $A \geq c$

Analyzing the Given Expression: " $7x8y + 638$ "

Clarification and Interpretation

The provided expression, $7x8y + 638$, seems to be a fragment or a typo. It's plausible that the intended expression is:

- $|7x + 8y| + 638$ (assuming an absolute value)
- or perhaps $|7x + 8y + 638|$ (more common in inequalities)
- or possibly $78y + 638$, which simplifies algebraically but doesn't involve an inequality.

Given the instruction to "rewrite the given inequality as two linear inequalities," the most typical context would involve an absolute value expression, such as:

$|7x + 8y + 638| < \text{some constant}$
or
 $|7x + 8y + 638| > \text{some constant}$

For illustrative purposes, let's assume the intended inequality is:

$|7x + 8y + 638| < c$

where c is a positive constant.

Transforming Absolute Value Inequalities into Linear Inequalities

Step 1: Isolate the Absolute Value Expression

Suppose we are given:

$|7x + 8y + 638| < c$

This inequality states that the expression $(7x + 8y + 638)$ is within a distance c from zero.

Step 2: Rewrite as a Compound Inequality

The fundamental property of absolute value inequalities states:

$$|A| < c \Leftrightarrow -c < A < c$$

Applying this to our expression:

$$-c < 7x + 8y + 638 < c$$

Similarly, if the inequality were:

$$|7x + 8y + 638| > c$$

then it would translate to:

$$7x + 8y + 638 < -c \text{ or } 7x + 8y + 638 > c$$

Practical Example: Rewriting an Absolute Value Inequality

Suppose the original inequality is:

$$|7x + 8y + 638| < 100$$

We can rewrite this as:

$$-100 < 7x + 8y + 638 < 100$$

Subtract 638 from all parts:

$$-100 - 638 < 7x + 8y < 100 - 638$$

Simplify:

$$-738 < 7x + 8y < -538$$

Thus, the original absolute value inequality is equivalent to the double linear inequality:

$$-738 < 7x + 8y < -538$$

Special Considerations and Edge Cases

When the Constant is Zero

If $c = 0$, then:

$$|7x + 8y + 638| < 0$$

But absolute value cannot be negative, so this inequality has no solutions. Conversely, if:

$$|7x + 8y + 638| \geq 0$$

which is always true, the solution set is the entire plane.

When the Inequality is a "Greater Than" or "Less Than" with Different Directions

- For $|A| > c$, the solution set is $A < -c$ or $A > c$.
- For $|A| < c$, the solution set is $-c < A < c$.

These distinctions are critical when solving inequalities involving absolute values, as they define different regions in the plane.

Visual Interpretation of the Solution Regions

Transforming absolute value inequalities into linear inequalities allows us to visualize the solution sets geometrically:

- Inequalities like $|7x + 8y + 638| < c$ correspond to the region between two parallel lines:
 $7x + 8y + 638 = c$ and $7x + 8y + 638 = -c$
- Inequalities like $|7x + 8y + 638| > c$ correspond to the region outside these lines.

Graphically, the boundary lines are straight, and the solution set is shaded accordingly, providing insight into feasible solutions.

Broader Implications and Applications

Understanding how to convert absolute value inequalities into linear inequalities is invaluable across various fields:

- Operations Research: Defining feasible regions within constraints.
- Engineering: Analyzing tolerances and error bounds.
- Economics: Modeling ranges of acceptable values.
- Data Science: Establishing thresholds for outlier detection.

This technique simplifies complex conditions into manageable, geometric, and algebraic forms, facilitating analysis, computation, and visualization.

Summary and Key Takeaways

- Absolute value inequalities can always be rewritten as two linear inequalities.

- The process involves understanding the fundamental properties of absolute values.
- The general transformation depends on whether the inequality involves “less than” or “greater than” signs.
- Visualizing the solution sets enhances comprehension and provides intuition about feasible regions.

Final Remarks

The process of translating an absolute value inequality into two linear inequalities exemplifies the power of algebraic manipulation in problem-solving. Although the initial expression in the prompt was somewhat ambiguous, the principles discussed are universally applicable. Mastery of these techniques equips students and professionals with tools to approach complex inequalities, analyze feasible regions, and interpret solutions in both theoretical and real-world contexts.

In future investigations, clarifying the initial expressions and constants involved will further streamline the problem-solving process. Nonetheless, the foundational concepts remain consistent, underscoring the importance of a solid grasp of absolute value inequalities and their transformations.

References

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Note: The actual specific inequality to be solved should be clarified for precise rewriting. The illustrative example provided demonstrates the general approach applicable to typical absolute value inequalities involving linear expressions.

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